

# Calculation Policy



Date: February 2022  
Review: February 2025

**Copyright of White Rose Maths**

Year 1 - 6

# Calculation Policy

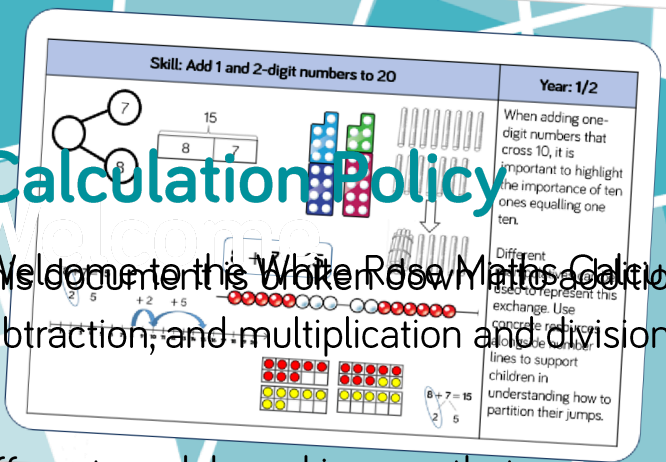
## Addition and Subtraction

**#MathsEveryoneCan**

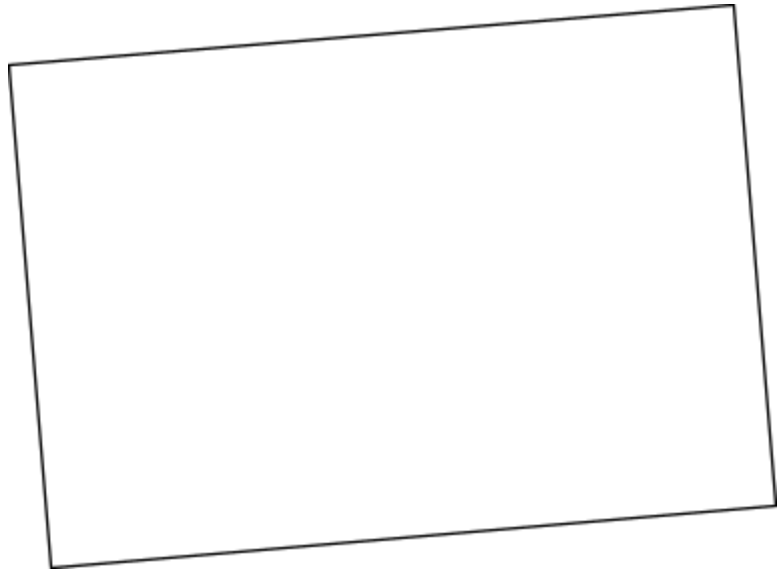


# Calculation Policy

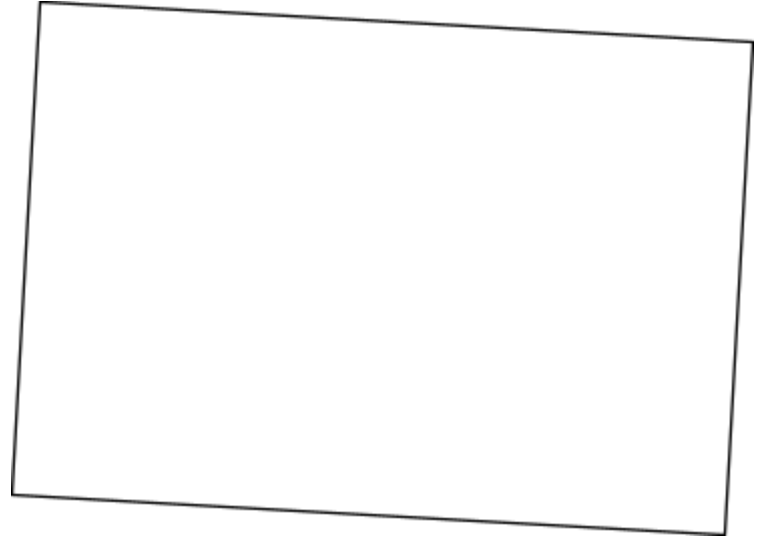
Welcome to the White Rose Maths Calculation Policy. This document covers addition and subtraction, and multiplication and division.



different models and images that can support the teaching of different concepts. These provide explanations of the benefits of using the models and show the links between different operations.



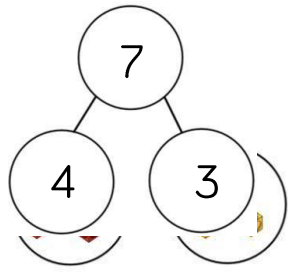
Each operation is then broken down into skills and each skill has a dedicated page showing the different models and images that could be used to effectively teach that concept.



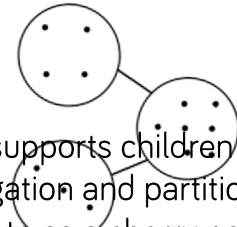
There is an overview of skills linked to year groups to support consistency through out school. A glossary of terms is provided at the end of the calculation policy to support understanding of the key language used to teach the four operations.



# Part-Whole Model



This model supports children in their aggregation and partitioning. Due to its shape, it is referred to as a cherry part-whole model.

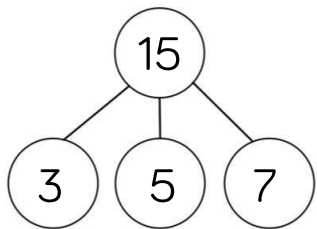


When the parts are complete and the whole is empty, children use aggregation to add the parts together to find the total.

$$7 = 4 + 3$$

$$- =$$

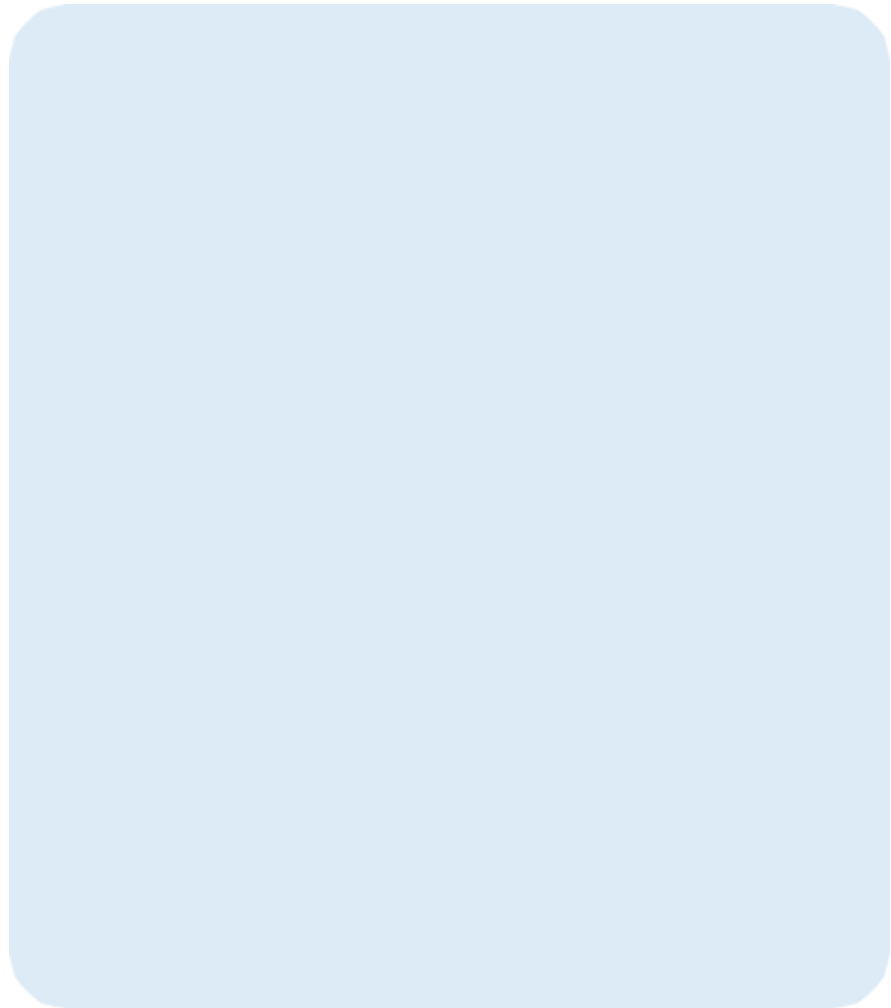
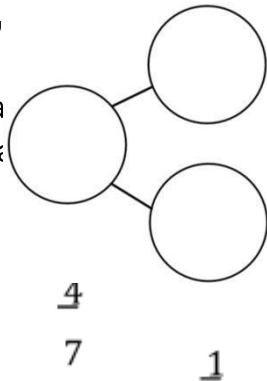
When the whole is complete and at least one of the parts is empty, children use partitioning (a form of subtraction).



This model is used to partition a number into tens and units.

This model is used to partition a number to help children to partition a number into tens and units.

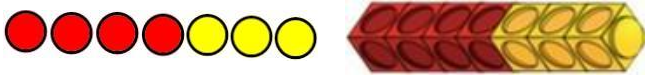
In KS2, children can use a part-whole model to help them understand the relationship between fractions, decimals and percentages.





# Part-Whole Model

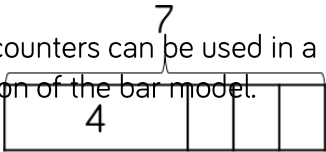
## Concrete



## Benefits

The single bar model is another type of a part-whole model that can support children in representing calculations to help them unpick the structure.

Cubes and counters can be used in a line as a concrete representation of the bar model.



Discrete bar models are a good starting point with smaller numbers. Each box represents one whole.

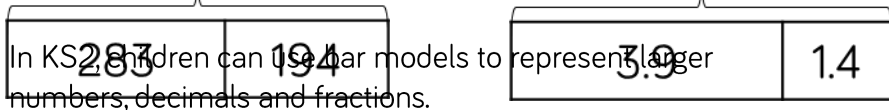
## Combination

The combination bar model can support children to calculate by counting on from the larger number. It's a good stepping stone towards the continuous bar model.

## Discrete

## Continuous

Continuous bar models are useful for a range of values. Each rectangle represents a number. The question mark indicates the value to be found.

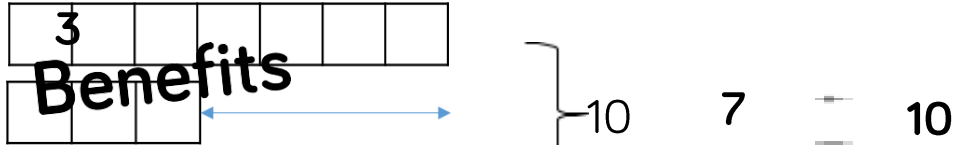


In KS2 children can use bar models to represent larger numbers, decimals and fractions.



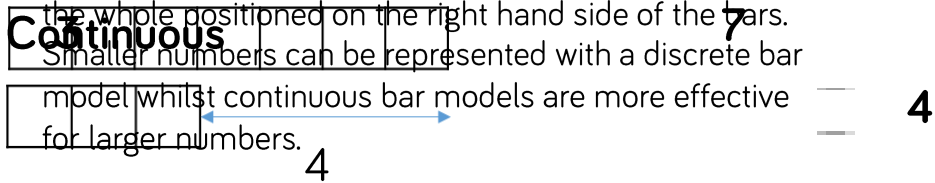
# Part-Whole Model

## Discrete



The multiple bar model is a good way to compare quantities whilst still unpicking the structure.

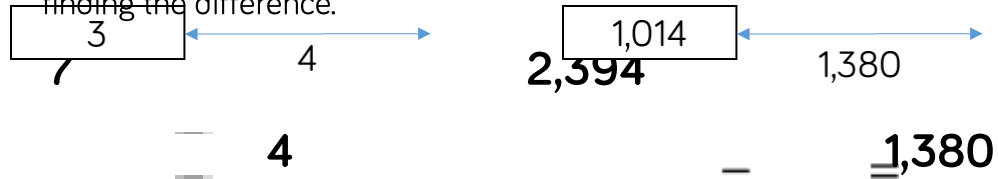
Two or more bars can be drawn, with a bracket labelling the whole positioned on the right hand side of the bars.



Smaller numbers can be represented with a discrete bar model whilst continuous bar models are more effective for larger numbers.

Multiple bar models can also be used to represent the difference in subtraction. An arrow can be used to model the difference.

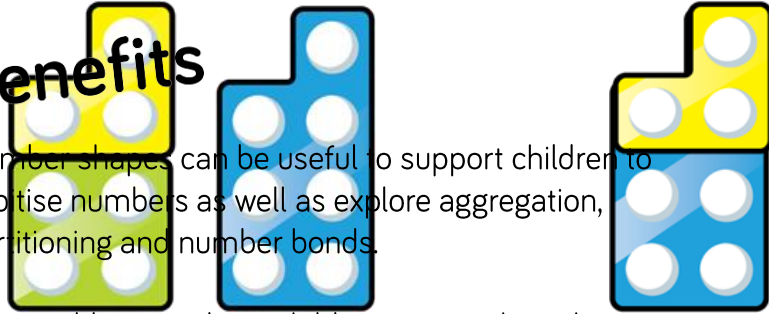
When working with smaller numbers, children can use cubes and a discrete model to find the difference. This supports children to see how counting on can help when finding the difference.



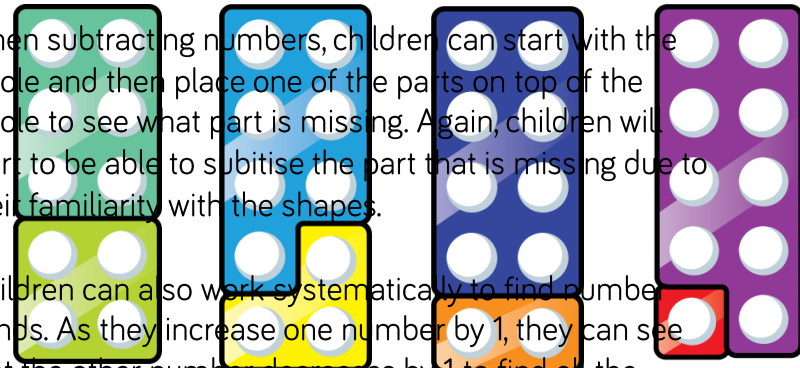
# Number Shapes

## Benefits

Number shapes can be useful to support children to subitise numbers as well as explore aggregation, partitioning and number bonds.

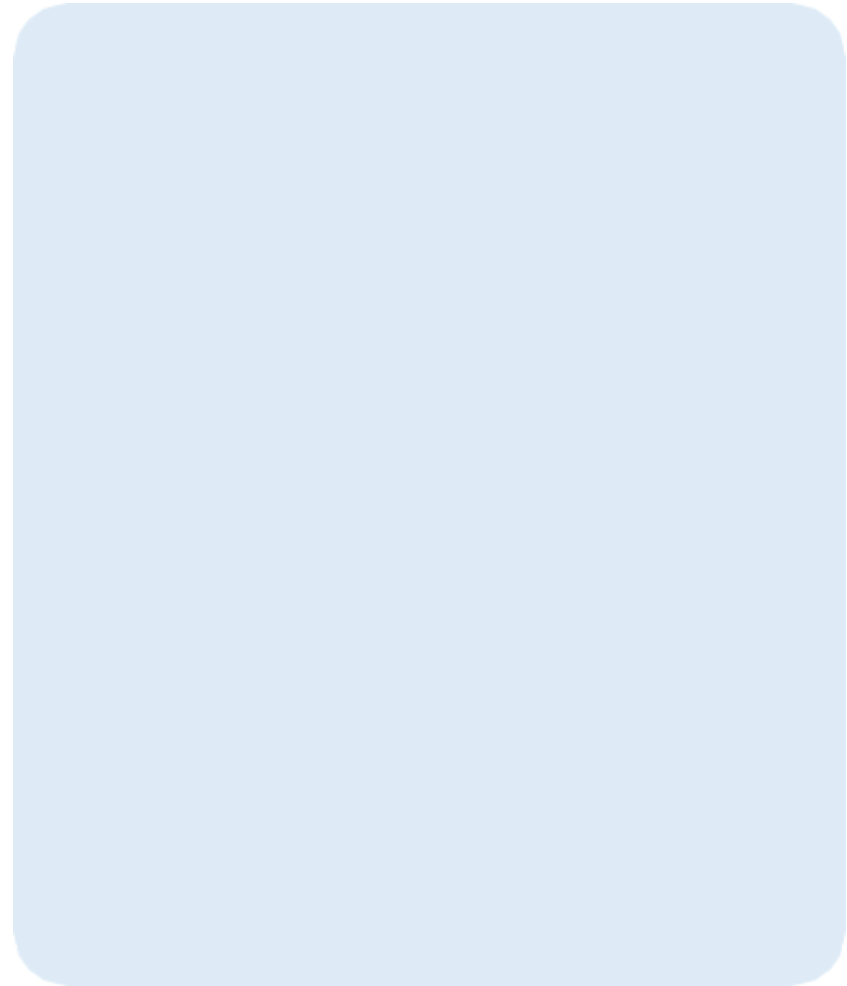


When adding numbers, children can see how the parts come together making a whole. As children use number shapes more often, they can start to subitise the total due to their familiarity with the shape of each number.



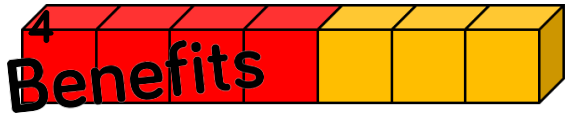
Children can also work systematically to find number bonds. As they increase one number by 1, they can see that the other number decreases by 1 to find all the possible number bonds for a number.

**6+4**      **7+3**      **8+2**      **9+1**



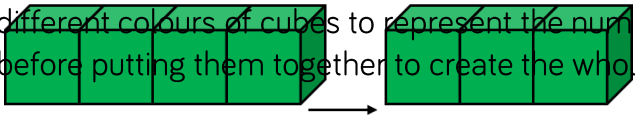
3

# Number Shapes

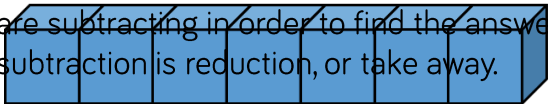


Cubes can be useful to support children with the addition and subtraction of one-digit numbers.

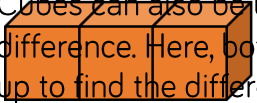
When adding numbers, children can see how the parts come together to make a whole. Children could use two different colours of cubes to represent the numbers before putting them together to create the whole.



When subtracting numbers, children can start with the whole and then remove the number of cubes that they are subtracting in order to find the answer. This model of subtraction is reduction, or take away.



Cubes can also be useful to look at subtraction as difference. Here, both numbers are made and then lined up to find the difference between the numbers.



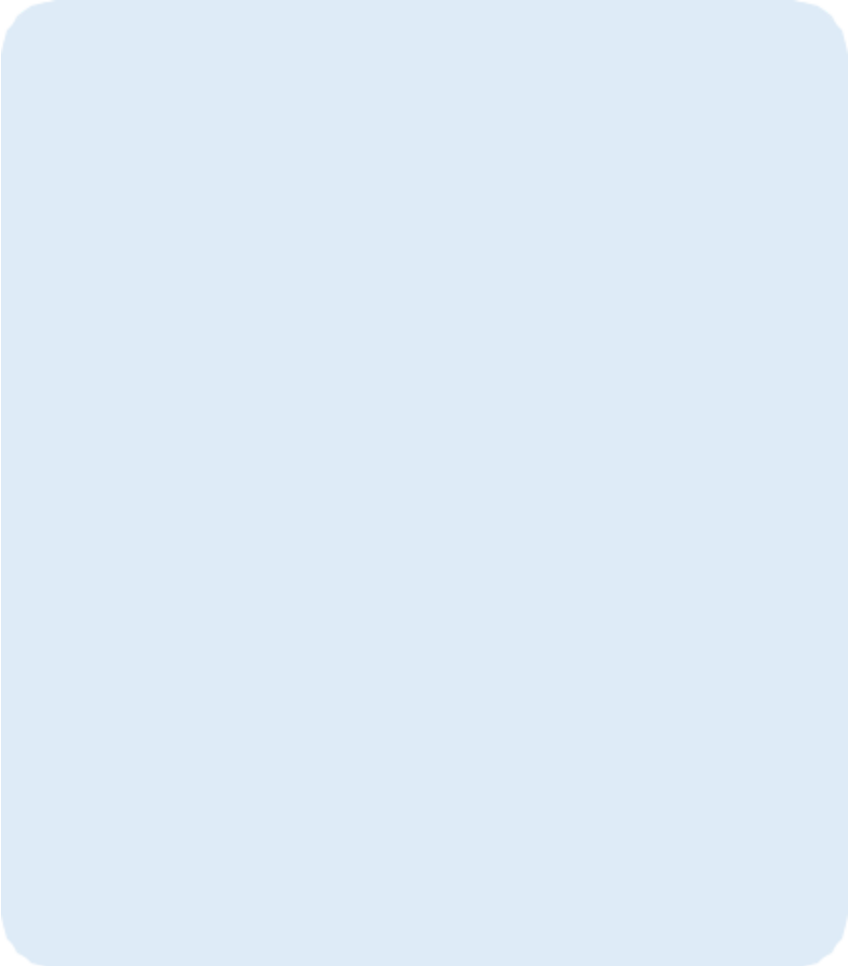
Cubes are useful when working with smaller numbers but are less efficient with larger numbers as they are difficult to subitise and children may miscount them.

4

4

3

4



# Number Shapes

7 is a part.

3 is a part.

7 is the whole.

3 is a part.

4 is a part.



When adding and subtracting within 10, the ten frame can support children to understand the different structures of addition and subtraction.

Using the language of parts and wholes represented by objects on the ten frame introduces children to aggregation and partitioning.

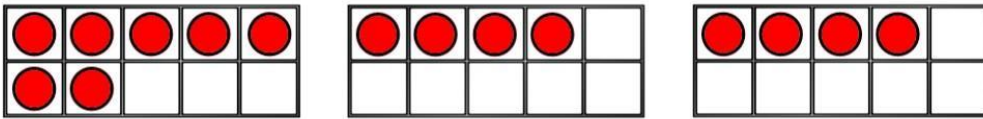


Aggregation is a form of addition where parts are combined together to make a whole. Partitioning is a form of subtraction where the whole is split into parts.

Using these structures, the ten frame can enable children to find all the number bonds for a number.

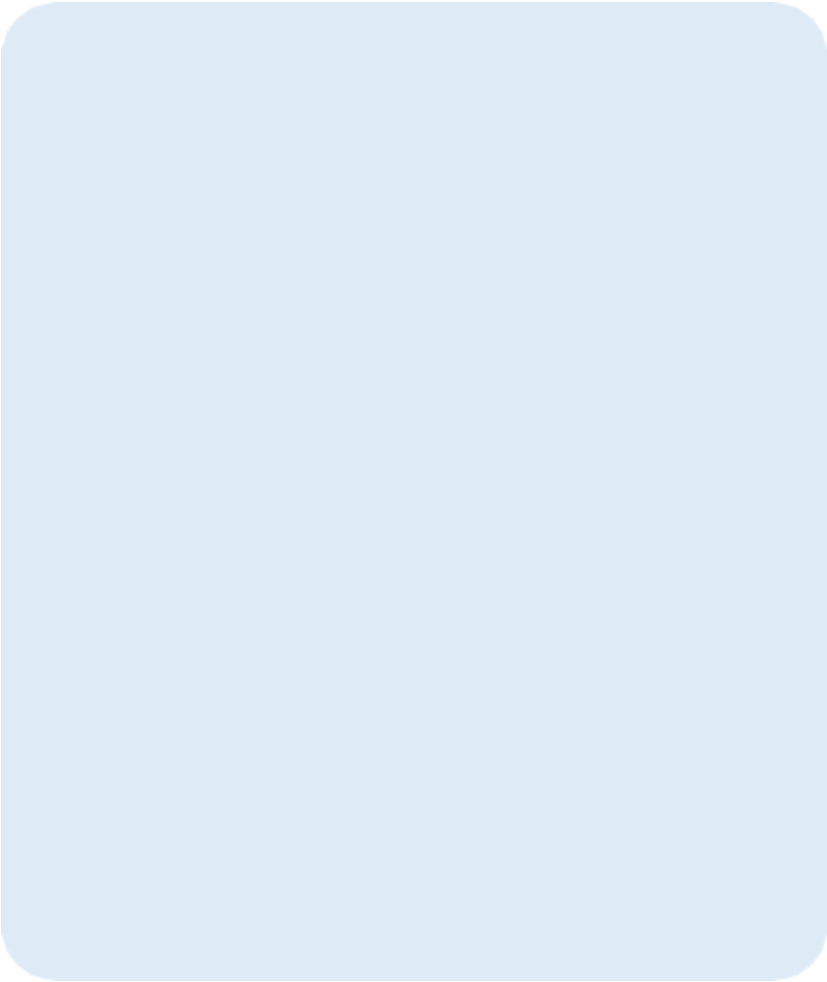
3 + 4 = 7

Children first also use ten frames to look at augmentation. Now

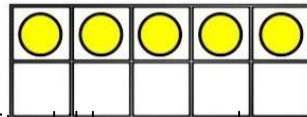
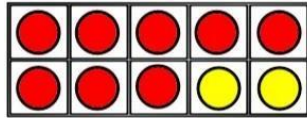
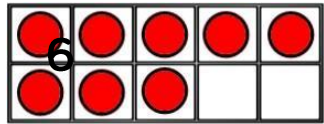


cars. Then, 3 cars left. Now, there are 4 cars.

3 + 1 = 4



# Ten Frames (within 20)



=

15

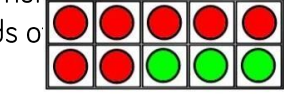
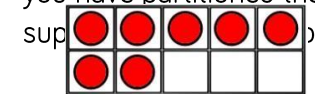
**Benefits**

When adding two single digits, children can make each number on separate ten frames before moving part of one number to make 10 on one of the ten frames. This

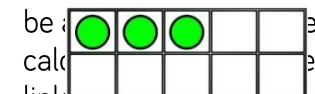
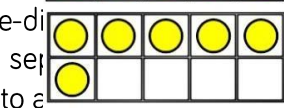
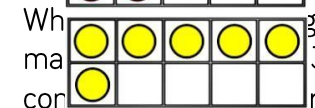
supports children to see how they have partitioned one of the numbers to make 10, and makes links to effective mental methods of addition.

When subtracting a one-digit number from a two-digit number, firstly make the larger number on 2 ten frames. Remove the smaller number, thinking carefully about how

you have partitioned the number to make 10 this



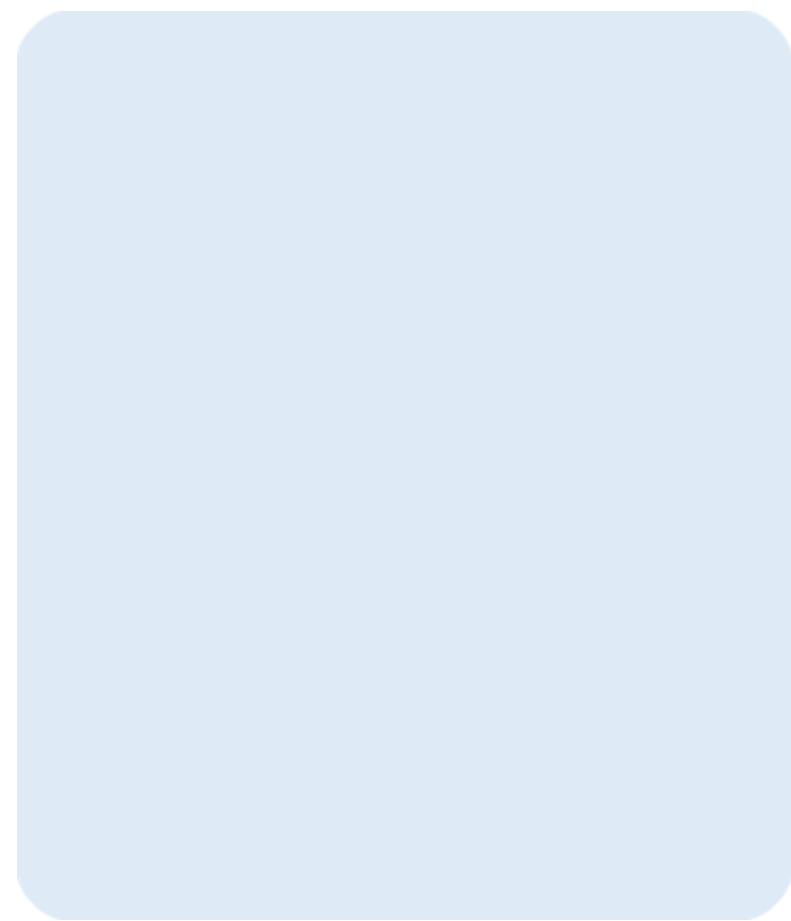
$$7 + 6 + 3 = 16$$



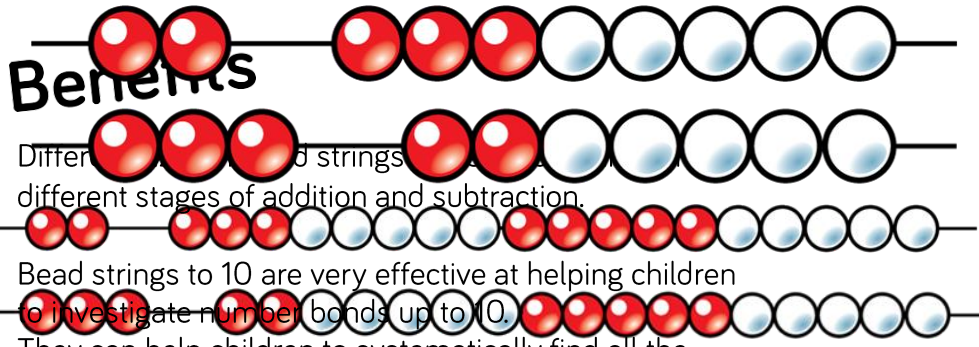
the importance of commutativity.

8

2



# Ten Frames (within 20)



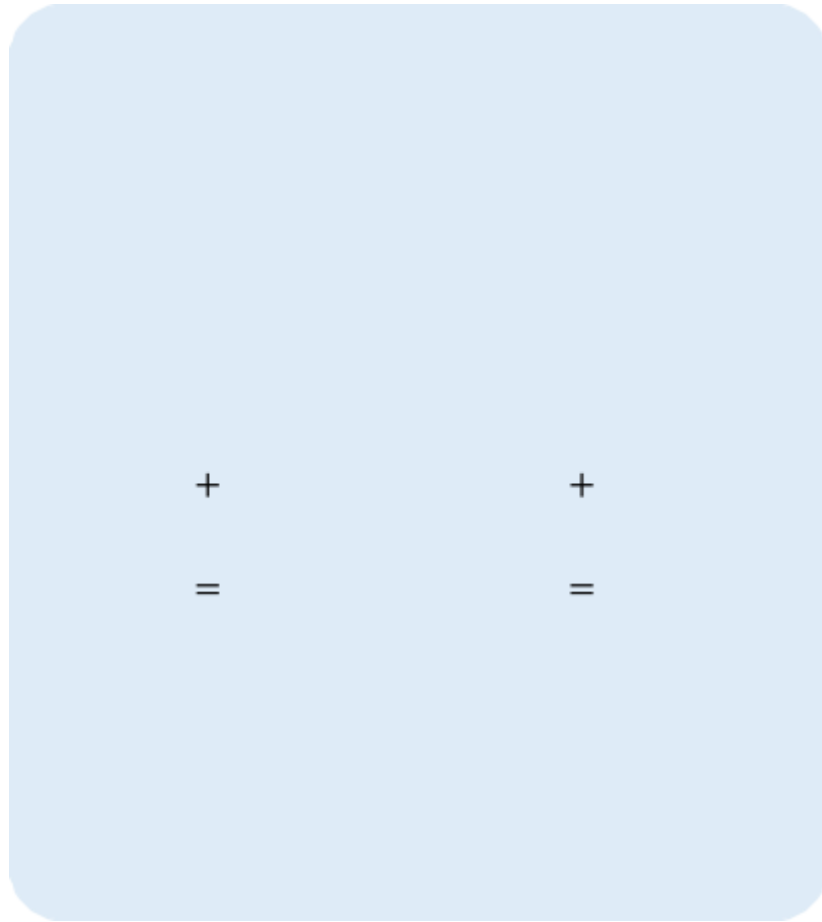
## Benefits

Different bead strings at different stages of addition and subtraction.

Bead strings to 10 are very effective at helping children to investigate number bonds up to 10. They can help children to systematically find all the number bonds to 10 by moving one bead at a time to see the different numbers they have partitioned the 10 beads into e.g. 2 + 8 = 10, move one bead, 3 + 7 = 10.

Bead strings to 20 work in a similar way but they also group the beads in fives. Children can apply their knowledge of number bonds to 10 and see the links to number bonds to 20.

Bead strings to 100 are grouped in tens and can support children in number bonds to 100 as well as helping when adding by making ten. Bead strings can show a link to adding to the next 10 on number lines which supports a mental method of addition.



# Ten Frames (within 20)

$$\begin{array}{r} + \\ - \\ \hline \end{array} 8$$

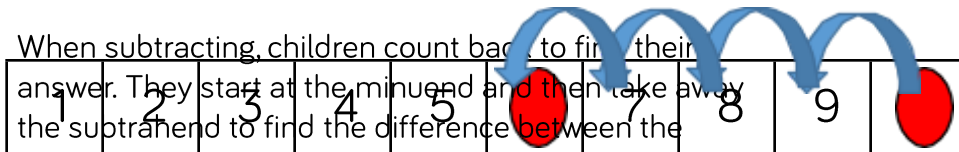
5

## Benefits



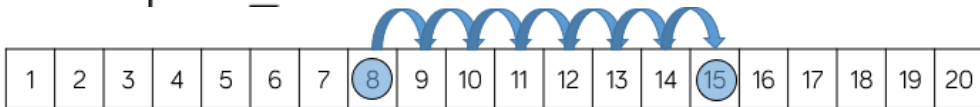
Number tracks are useful to support children in their understanding of augmentation and reduction.

When adding, children count on to find the total of the numbers. On a number track, children can place a counter on the starting number and then count on to find the total.



When subtracting, children count back to find their answer. They start at the minuend and then take away the subtrahend to find the difference between the numbers.

Number tracks can work well alongside ten frames and bead strings which can also model counting on or counting back.



track before they move on to number lines.

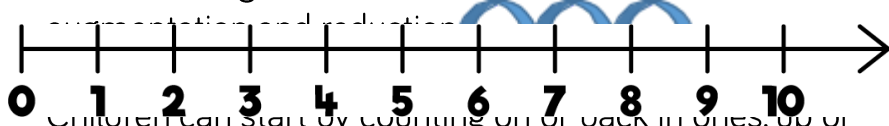




# Benefits

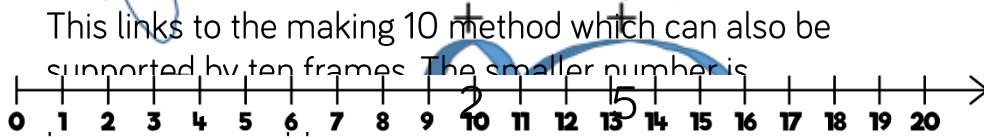
Number Lines (within 20)

Labelled number lines support children in their understanding of addition and subtraction as **counting on and back**.



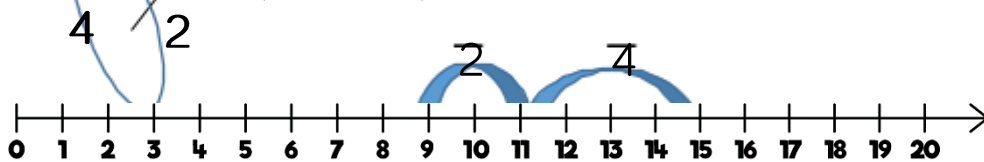
Children can start by counting on or back in ones, up or down the number line. This skill links directly to the use of the number track.

Progressing further, children can add numbers by jumping to the nearest 10 and then jumping to the total. This links to the making 10 method which can also be supported by ten frames.



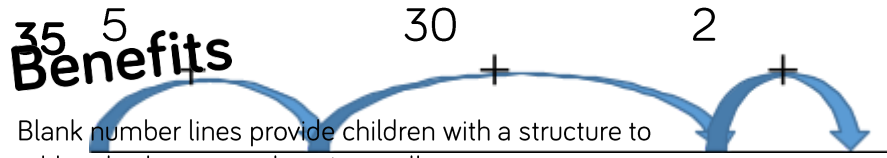
The smaller number is to 10 and to then add on the remaining part.

Children can subtract numbers by firstly jumping to the nearest 10. Again, this can be supported by ten frames so children can see how they partition the smaller number into the two separate jumps.



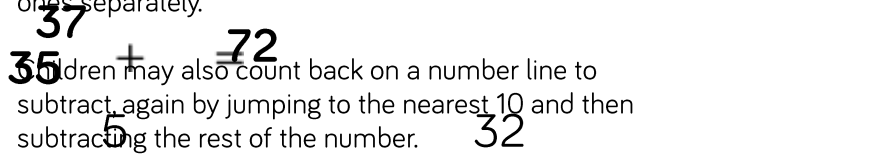
# Ten Frames (within 20)

$$37 + \quad = 72$$

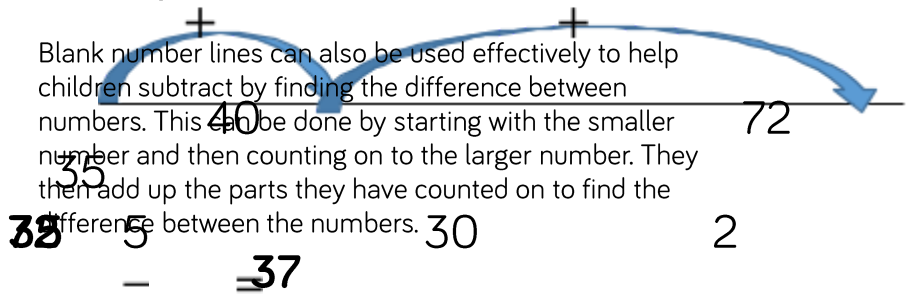


Blank number lines provide children with a structure to add and subtract numbers in smaller parts.

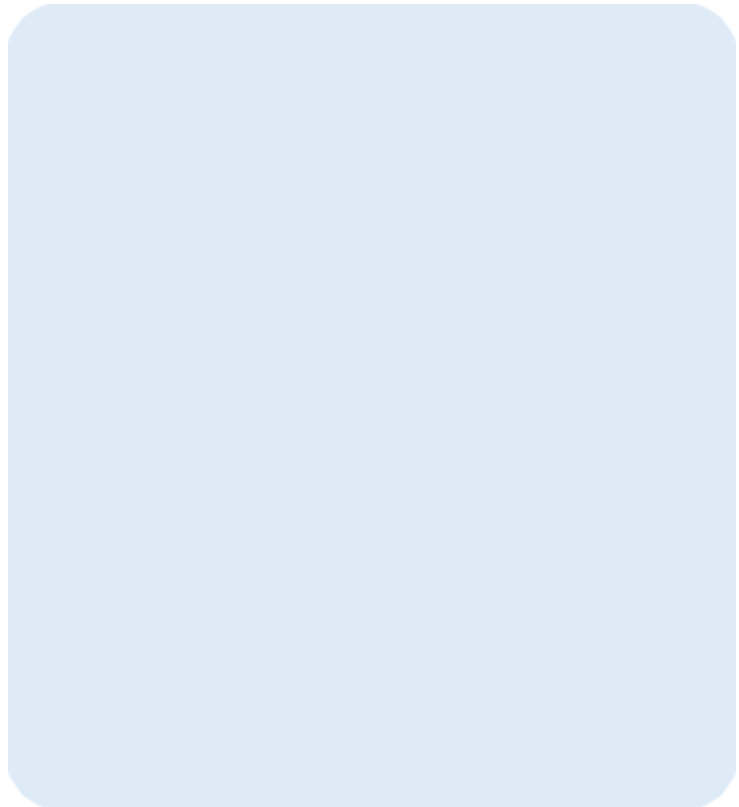
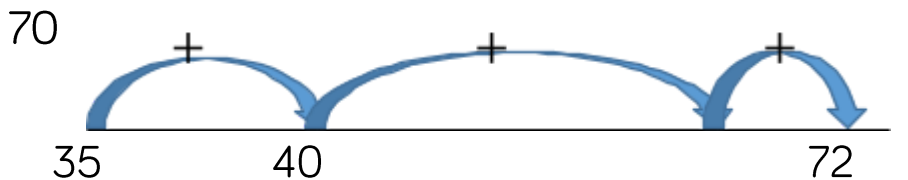
Developing from labelled number lines, children can add by jumping to the nearest 10 and then adding the rest of the number either as a whole or by adding the tens and ones separately.



Children may also count back on a number line to subtract, again by jumping to the nearest 10 and then subtracting the rest of the number.

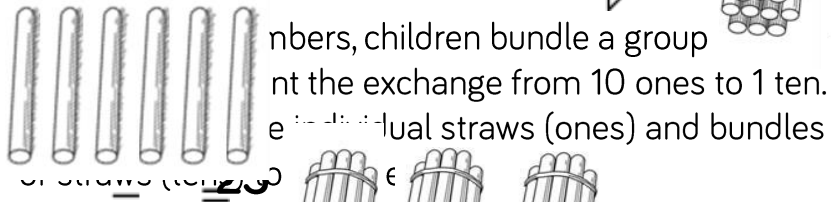
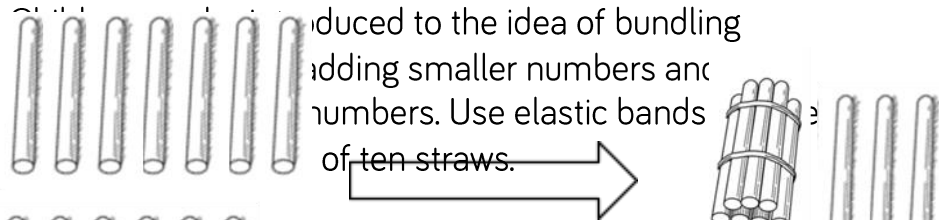


Blank number lines can also be used effectively to help children subtract by finding the difference between numbers. This can be done by starting with the smaller number and then counting on to the larger number. They then add up the parts they have counted on to find the difference between the numbers.

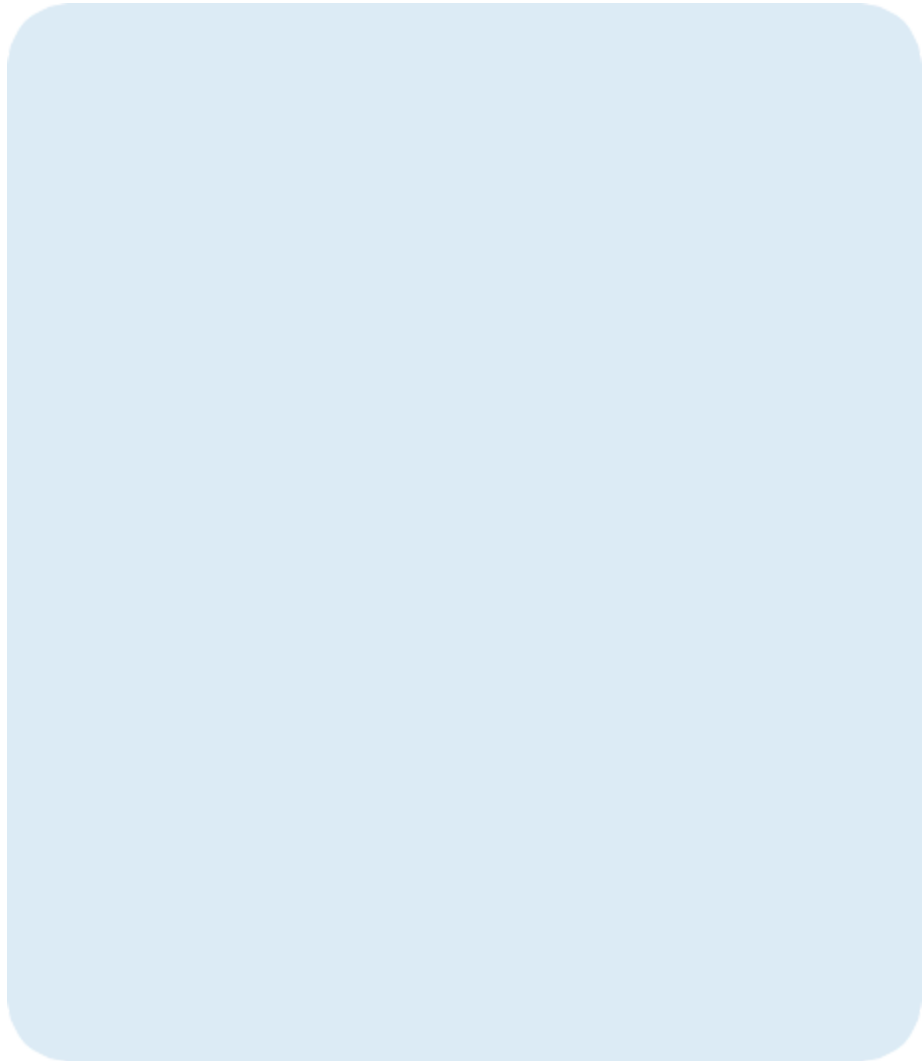
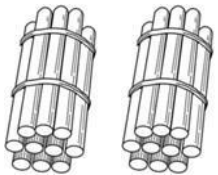
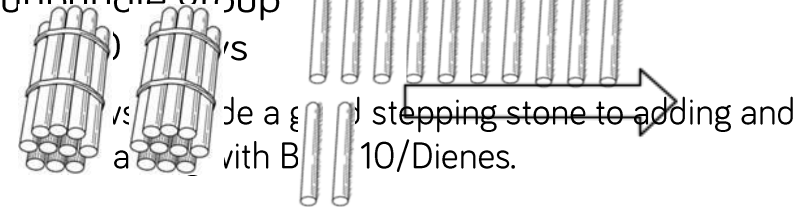


# Bundle together benefits

Straws are an effective way to support children in their understanding of exchange when adding and subtracting 2-digit numbers.



When subtracting 1 ten from a group of 10 straws to represent 1 ten to 10



# Ten Frames (within 20)

20

Tens	Ones
61	

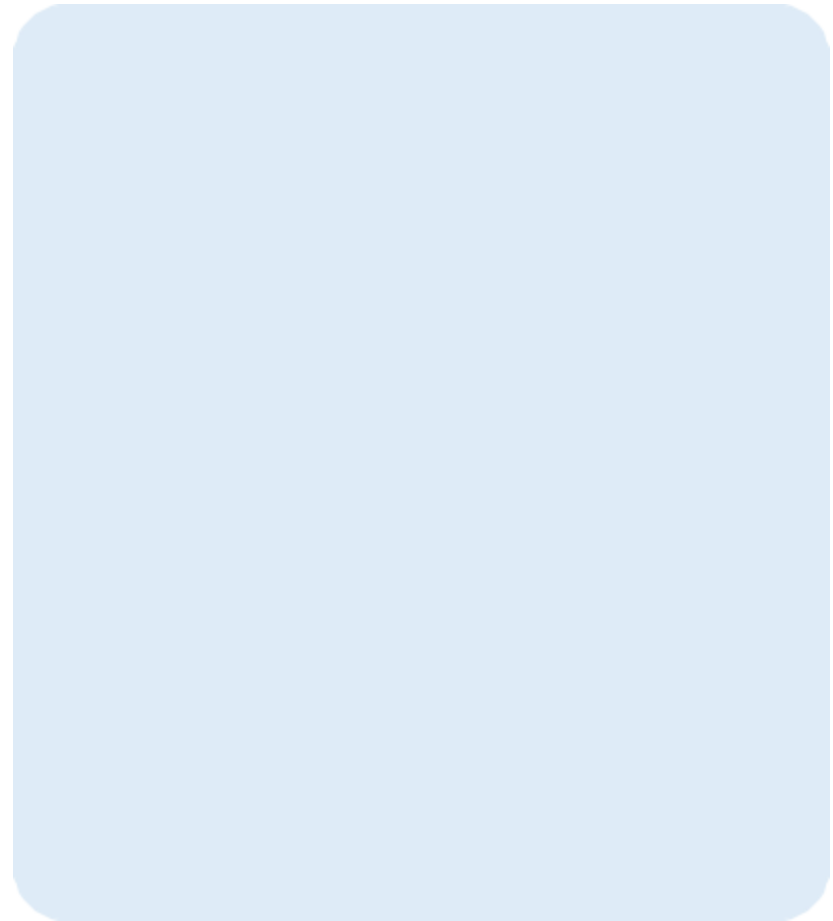
to support  
n. It is  
ulations  
y can see the  
d the model.

$$\begin{array}{r} + \\ \hline 1 \end{array}$$

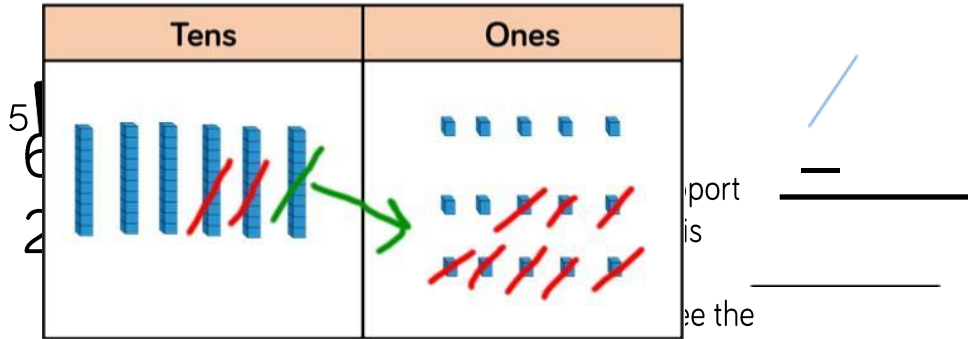
change before moving on to addition with exchange. The representation becomes less efficient with larger numbers due to the

Hundreds	Tens	Ones
429		

be  
ie  
+  
1

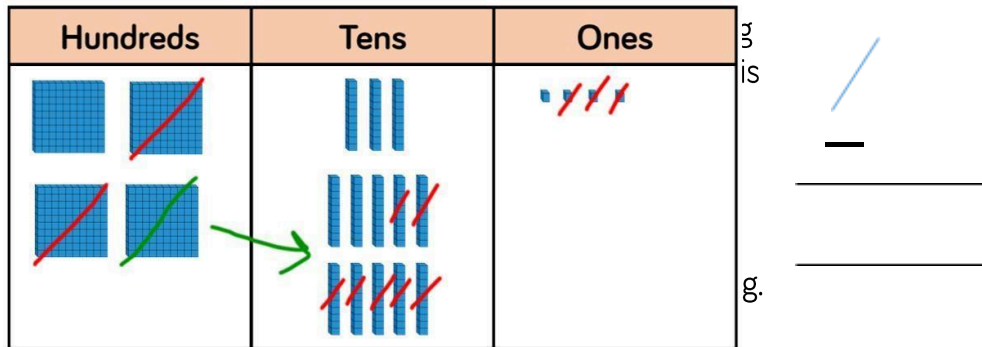


# Ten Frames (within 20)



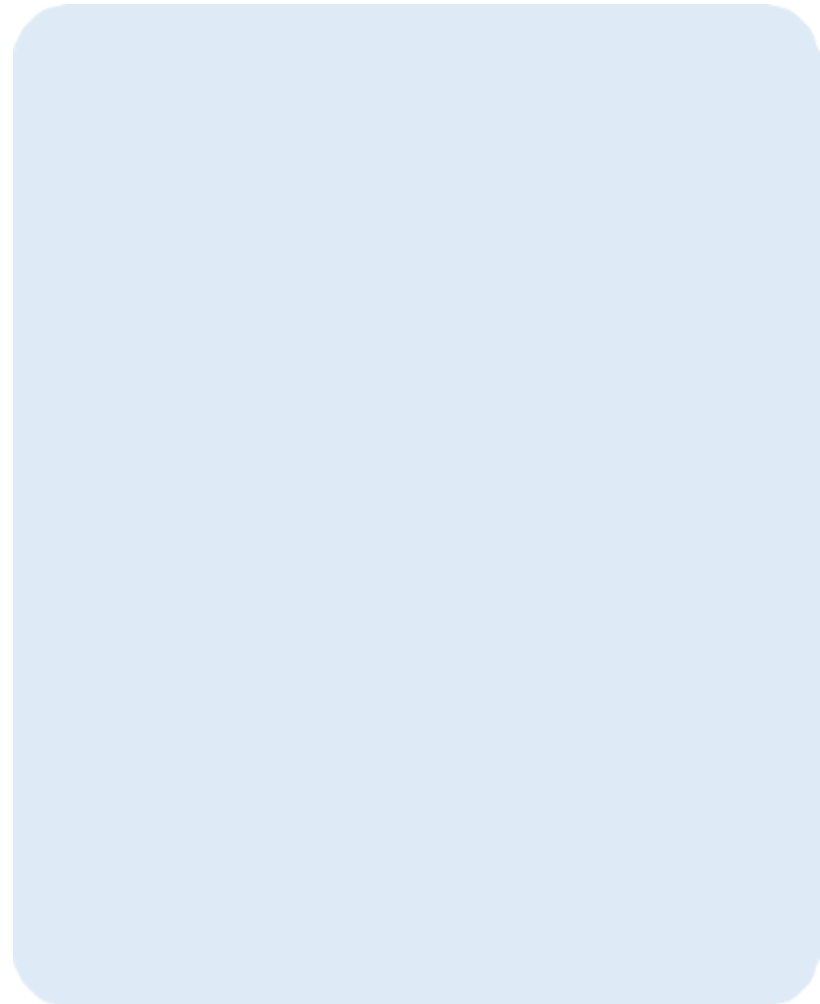
clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. When building



efficiently.

This model is efficient with up to 4-digit numbers. Place value counters are more efficient with larger numbers and decimals.



# Ten Frames (within 20)

Hundreds	Tens	Ones
100 100 100	10 10 10 10 10 10 10 10	1 1 1 1
100 100	10 10 10	1 1 1 1 1 1 1

100

10

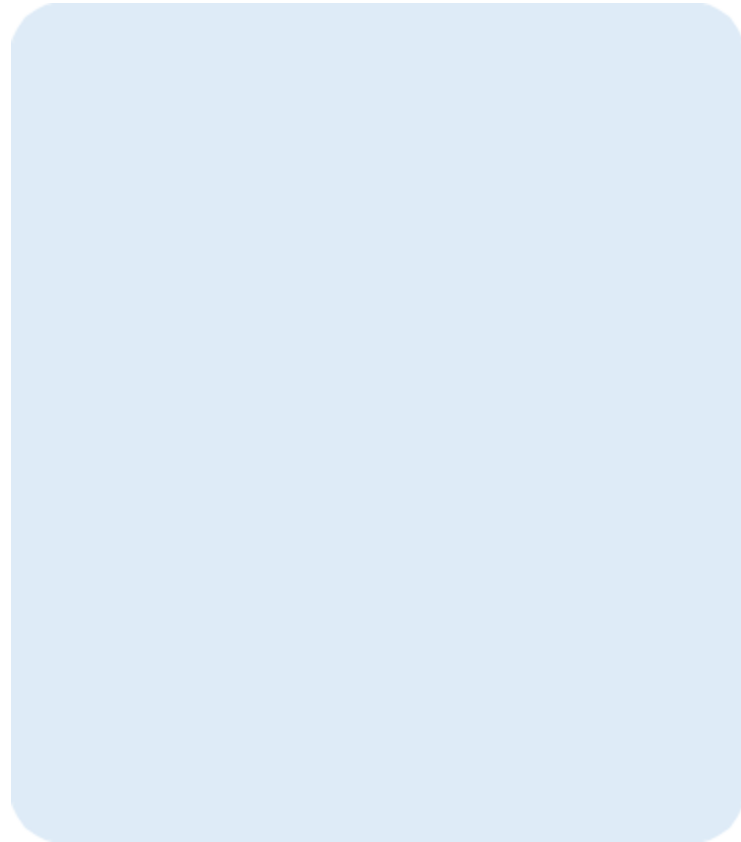
Moving on to addition with exchange. Different place value counters can be used to represent larger numbers or decimals. If you don't have place value counters, use normal counters on a place value grid to enable children

Ones	Tenths	Hundredths
1 1 1	0.1 0.1 0.1 0.1 0.1 0.1	0.01 0.01 0.01 0.01 0.01
1 6.06	0.1 0.1 0.1 0.1	0.01

1

$$\begin{array}{r}
 + \\
 \hline
 11
 \end{array}$$

$$\begin{array}{r}
 + \\
 \hline
 1
 \end{array}$$



# Place Value and Counters (Subtraction)

## Benefits

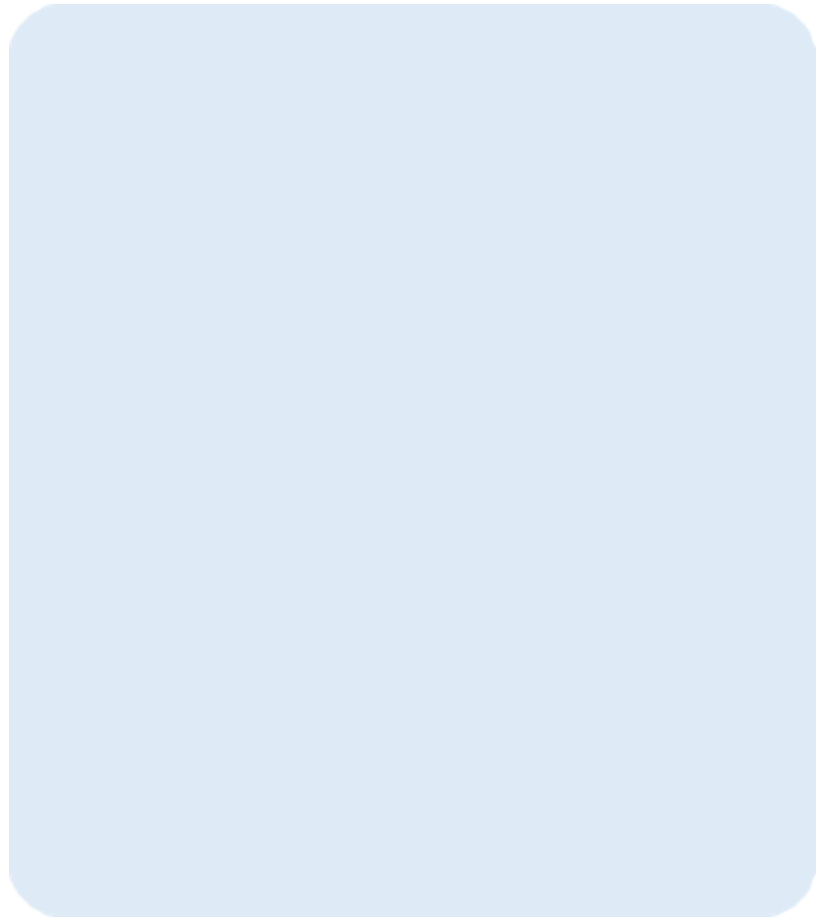
Hundreds	Tens	Ones

support  
is  
s  
see the  
model.  
e before

moving on to subtraction with exchange. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns

Thousands	Hundreds	Tens	Ones

ds  
s





**Addition**



## Representations and models

Add two 1-digit numbers to 10

Part-whole model  
Bar model  
Number shapes

Ten frames (within 10)  
Bead strings (10)  
Number tracks

Add 1 and 2-digit numbers to 20

Part-whole model  
Bar model  
Number shapes  
Ten frames (within 20)

Bead strings (20)  
Number tracks  
Number lines (labelled)  
Straws

Add three 1-digit numbers

Part-whole model  
Bar model

Ten frames (within 20)  
Number shapes

Add 1 and 2-digit numbers to 100

Part-whole model  
Bar model  
Number lines (labelled)

Number lines (blank)  
Straws  
Hundred square

## Representations and models

Add two 2-digit numbers

Part-whole model  
Bar model  
Number lines (blank)  
Straws

Base 10  
Place value counters  
Column addition

Add with up to 3-digits

Part-whole model  
Bar model

Base 10  
Place value counters  
Column addition

Add with up to 4-digits

Part-whole model  
Bar model

Base 10  
Place value counters  
Column addition

Add with more than 4 digits

Part-whole model  
Bar model

Place value counters  
Column addition

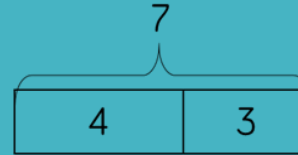
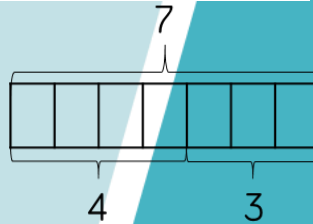
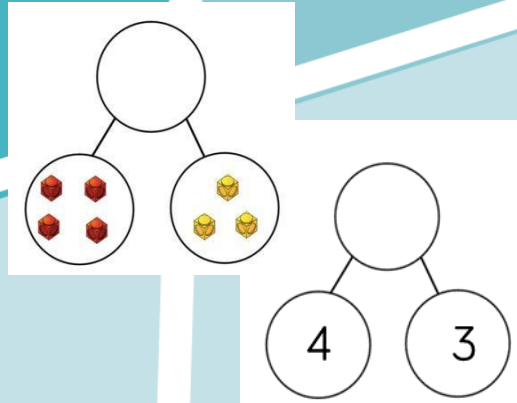
Add with up to 3 decimal places

Part-whole model  
Bar model

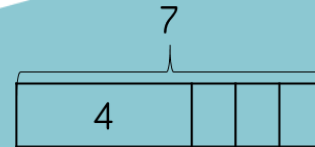
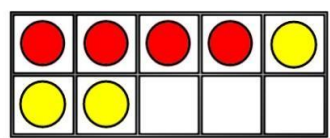
Place value counters  
Column addition

# Skill: Add 1-digit numbers within 10

Year: 1



4 3 7



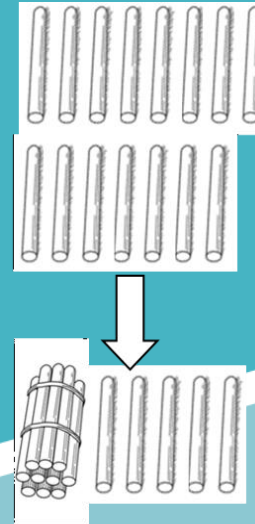
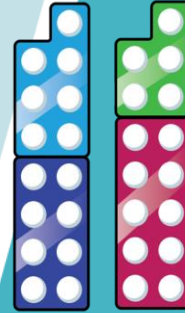
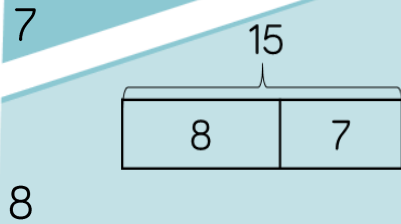
When adding numbers to 10, children can explore both aggregation and augmentation.

The part-whole model, discrete and continuous bar model, number shapes and ten frame support aggregation.

The combination bar model, ten frame, bead string and number track all support augmentation.

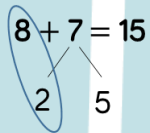
# Skill: Add 1 and 2-digit numbers to 20

Year: 1/2

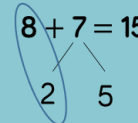
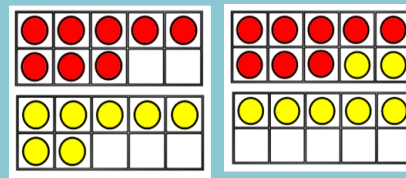
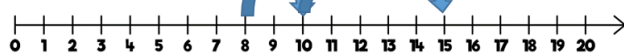


When adding one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten.

8 7 15



+2 +5



Different manipulatives can be used to represent this exchange. Use concrete resources alongside number lines to support children in understanding how to partition their jumps.

## Skill: Add three 1-digit numbers

Year: 2

When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add the numbers more efficiently.

This supports children in their understanding of commutativity.

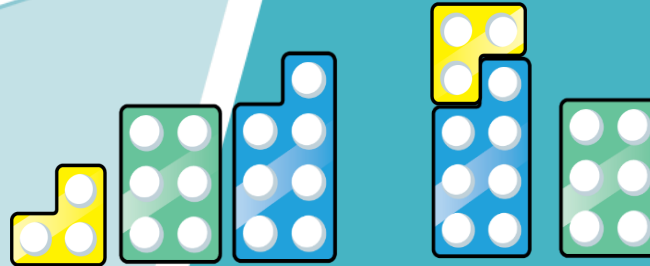
16 Manipulatives that highlight number bonds to 10 are effective when adding three 1-digit numbers.

16

7

6

3

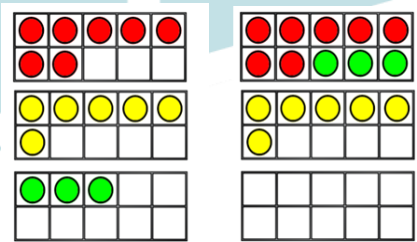


7

6

3

16

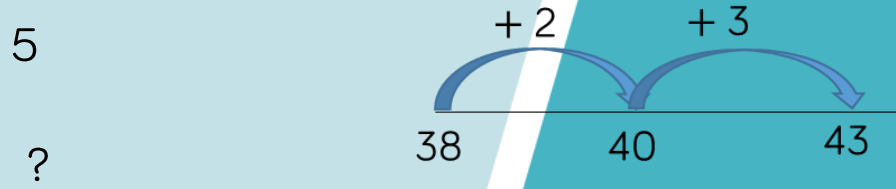
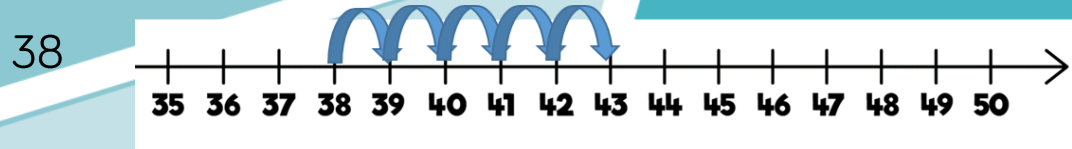


$$7 + 6 + 3 = 16$$

10

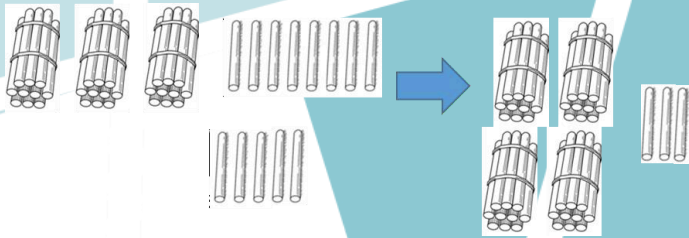
## Skill: Add 1-digit and 2-digit numbers to 100

Year: 2/3



38

38 5 43



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

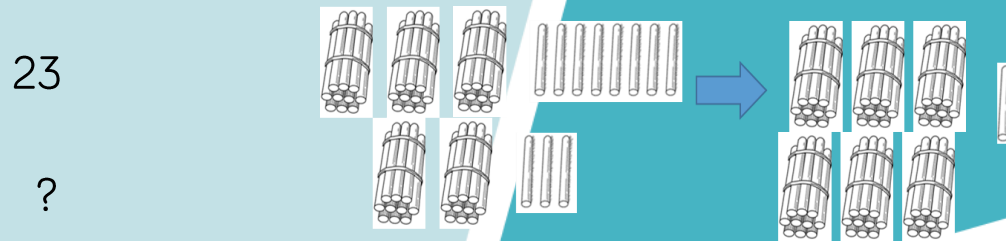
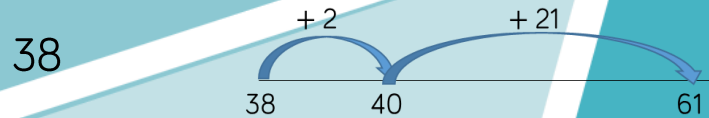
When adding single digits to a two-digit number, children should be encouraged to count on from the larger number.

They should also apply their knowledge of number bonds to add more efficiently e.g. 8 5 13 so 38 5 43.

Hundred squares and straws can support children to find the number bond to 10.

## Skill: Add two 2-digit numbers to 100

Year: 2/3



38            23            38            23            61

At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.

Children can also use a blank number line to count on to find the total. Encourage them to jump to multiples of 10 to become more efficient.

Tens	Ones

$$\begin{array}{r} 38 \\ + 23 \\ \hline 61 \\ 1 \end{array}$$

Tens	Ones

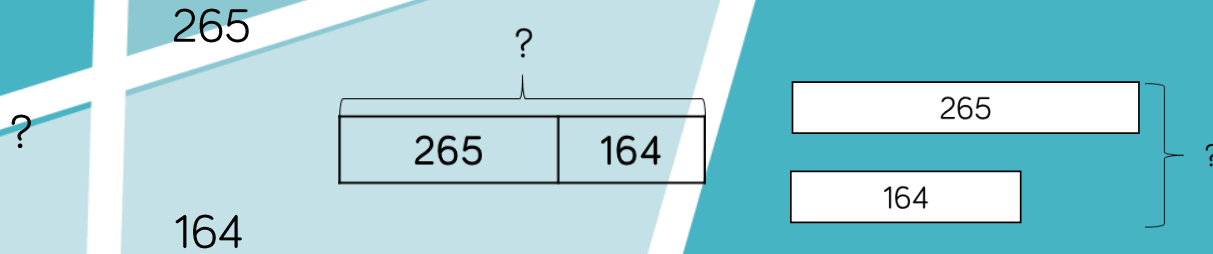
## Skill: Add numbers with up to 3 digits

**Year: 3**

Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.



$$265 + 164 = 429$$

Hundreds	Tens	Ones

$$\begin{array}{r} 265 \\ + 164 \\ \hline 429 \\ \hline 1 \end{array}$$

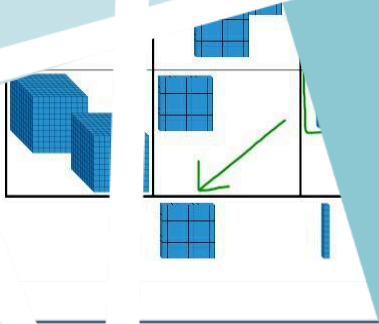
Hundreds	Tens	Ones



**Skill: Add numbers with up to 4 digits**

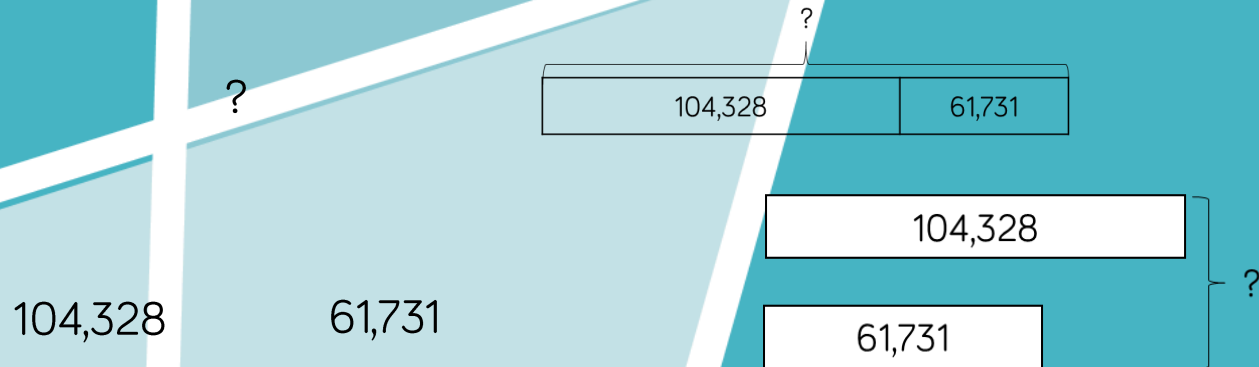
**Year: 4**

Base 10 and place



**Skill: Add numbers with more than 4 digits**

**Year: 5/6**



$$104,328 + 61,731 = 166,059$$

Place value counters or plain counters on a place value grid are the most effective concrete resources when adding numbers with more than 4 digits.

At this stage, children should be encouraged to work in the abstract, using the column method to add larger numbers efficiently.

HTh	TTh	Th	H	T	O
100,000		1,000 1,000 1,000 1,000	100 100 100	10 10	1 1 1 1 1 1 1 1
	10,000 10,000 10,000 10,000 10,000 10,000	1,000	100 100 100 100 100 100 100	10 10 10	1

1	0	4	3	2	8
+	6	1	7	3	1
1	6	6	0	5	9
			1		

## Skill: Add with up to 3 decimal places

Year: 5

2.41

3.65

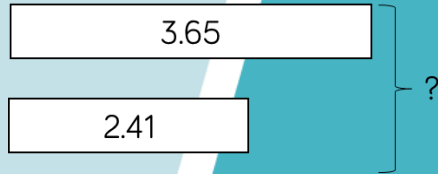
?

3.65

2.41

$$\begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ 1 \end{array}$$

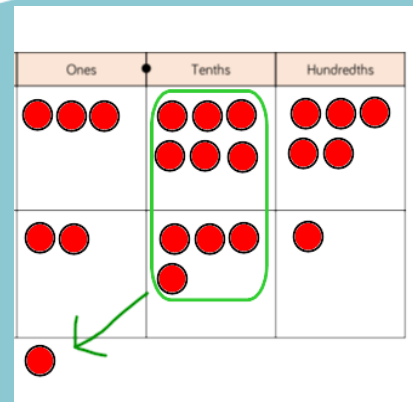
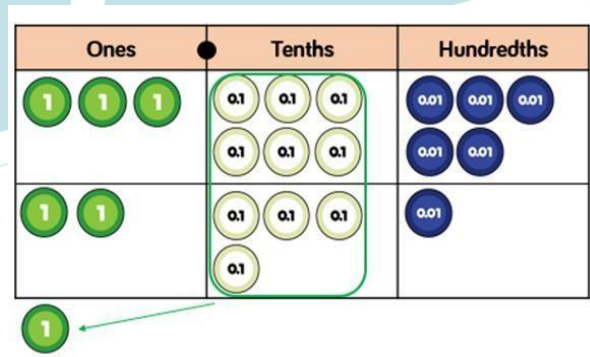
?



3.65    2.41    6.06

Place value counters and plain counters on a place value grid are the most effective manipulatives when adding decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of adding decimals with a variety of decimal places. This includes putting this into context when adding money and other measures.





**Subtraction**

## Representations and models

Subtract two 1-digit numbers to 10

Part-whole model  
Bar model  
Number shapes

Ten frames (within 10)  
Bead strings (10)  
Number tracks

Subtract 1 and 2-digit numbers to 20

Part-whole model  
Bar model  
Number shapes  
Ten frames (within 20)

Bead string (20)  
Number tracks  
Number lines (labelled)  
Straws

Subtract 1 and 2-digit numbers to 100

Part-whole model  
Bar model  
Number lines (labelled)

Number lines (blank)  
Straws  
Hundred square

Subtract two 2-digit numbers

Part-whole model  
Bar model  
Number lines (blank)  
Straws

Base 10  
Place value counters  
Column addition





## Representations and models

Subtract with up to 3-  
digits

Part-whole model  
Bar model

Base 10  
Place value counters  
Column addition

Subtract with up to 4-  
digits

Part-whole model  
Bar model

Base 10  
Place value counters  
Column addition

Subtract with more than  
4 digits

Part-whole model  
Bar model

Place value counters  
Column addition

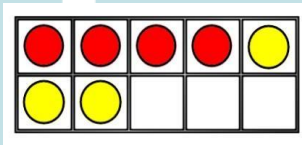
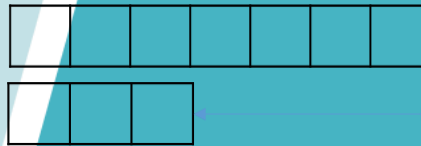
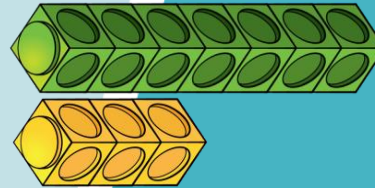
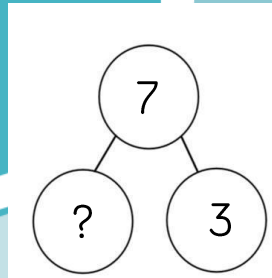
Subtract with up to 3  
decimal places

Part-whole model  
Bar model

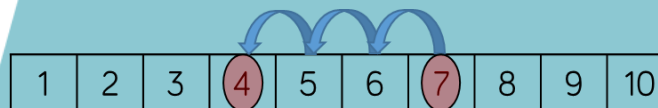
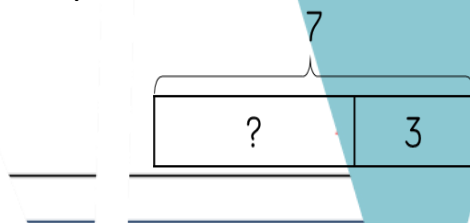
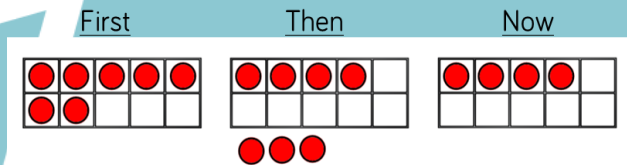
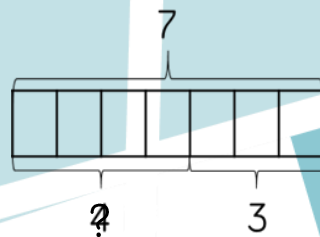
Place value counters  
Column addition

# Skill: Subtract 1-digit numbers within 10

Year: 1



7 3 4



Part-whole models, bar models, ten frames and number shapes support partitioning.

Ten frames, number tracks, single bar models and bead strings support reduction.

Cubes and bar models with two bars can support finding the difference.

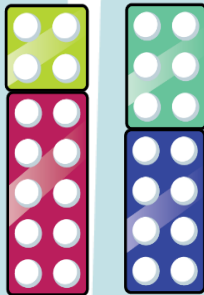
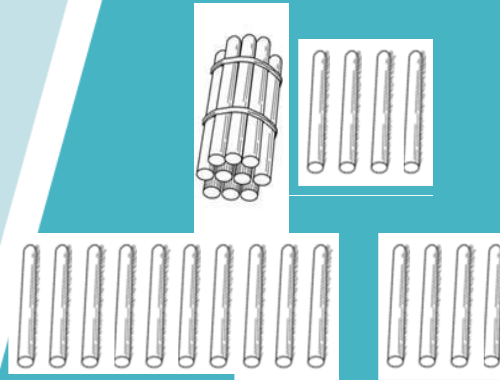
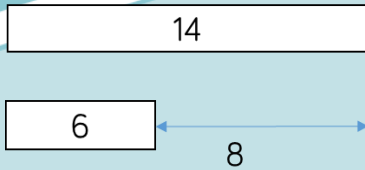


# Skill: Subtract 1 and 2-digit numbers to 20

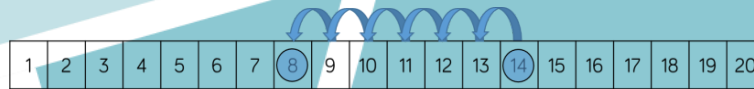
Year: 1/2

6

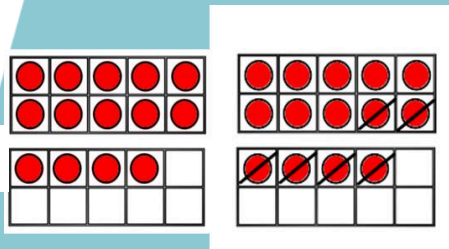
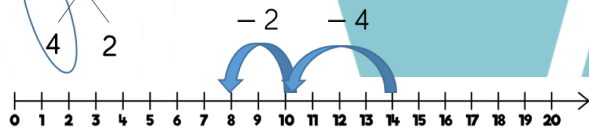
14



14 6 8



$$14 - 6 = 8$$



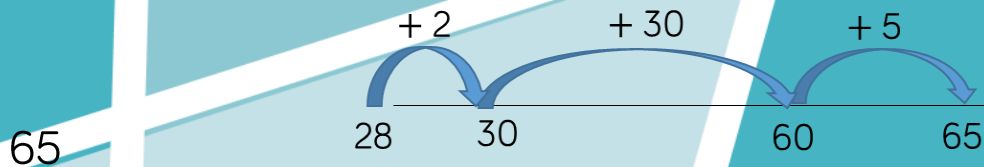
$$14 - 6 = 8$$

When subtracting one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten.

Children should be encouraged to find the number bond to 10 when partitioning the subtracted number. Ten frames, number shapes and number lines are particularly useful for this.

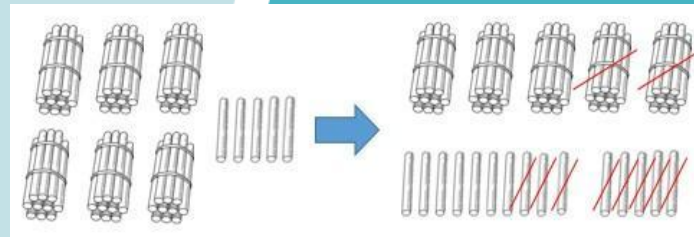
## Skill: Subtract 1 and 2-digit numbers to 100

**Year: 2**



28

65



?

28

65

28

37

Tens	Ones

$$\begin{array}{r} 5 \ 1 \\ 65 \\ - 28 \\ \hline 37 \end{array}$$

Tens	Ones

At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.

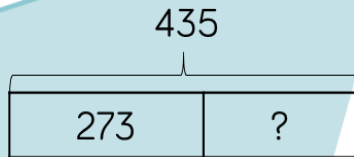
Children can also use a blank number line to count on to find the difference. Encourage them to jump to multiples of 10 to become more efficient.

## Skill: Subtract numbers with up to 3 digits

Year: 3

435  
273

?

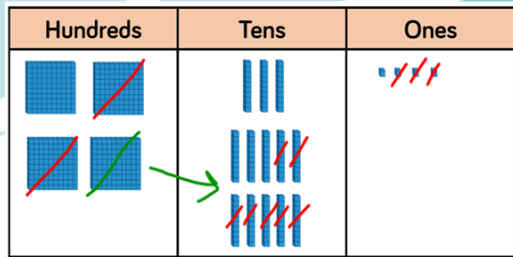


435    273    262

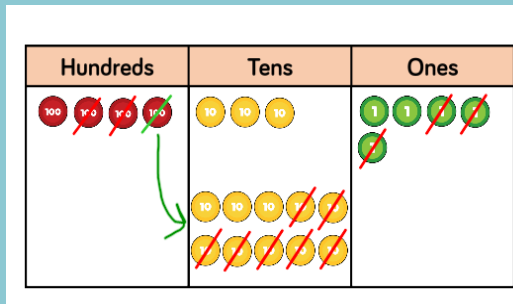
Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.



$$\begin{array}{r} 3 \quad 1 \\ 435 \\ - 273 \\ \hline 262 \end{array}$$



## Skill: Subtract numbers with up to 4 digits

Year: 4

4,357

2,735

?

4,357

2,735

?

4,357

2,735

?

$$\begin{array}{r} 4,357 \\ - 2,735 \\ \hline 1,622 \end{array}$$

Base 10 and place value counters are the most effective manipulatives when subtracting numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

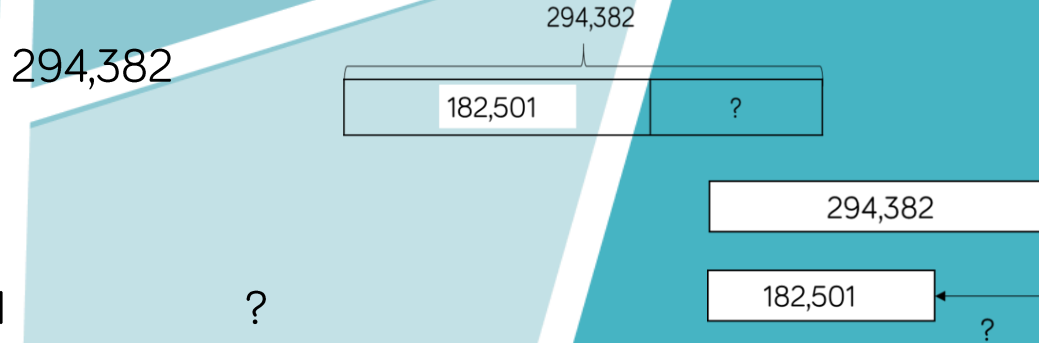
4,357    2,735    1,622

Thousands	Hundreds	Tens	Ones

Thousands	Hundreds	Tens	Ones

## Skill: Subtract numbers with more than 4 digits

Year: 5/6



Place value counters or plain counters on a place value grid are the most effective concrete resource when subtracting numbers with more than 4 digits.

$$294,382 - 182,501 = 111,881$$

HTh	TTh	Th	H	T	O
<del>100,000</del> <del>100,000</del>	<del>10,000</del> <del>10,000</del> <del>10,000</del> <del>10,000</del> <del>10,000</del> <del>10,000</del> <del>10,000</del> <del>10,000</del> <del>10,000</del>	<del>1,000</del> <del>1,000</del> <del>1,000</del> <del>1,000</del>	100 100 100 100 100 100 <del>100</del> <del>100</del> <del>100</del> <del>100</del> <del>100</del> <del>100</del> <del>100</del>	10 10 10 10 10 10 10 10	<del>1</del> <del>1</del>

	2	9	<del>3</del>	13	8	2
-	1	8	2	5	0	1
	1	1	1	8	8	1

At this stage, children should be encouraged to work in the abstract, using column method to subtract larger numbers efficiently.

## Skill: Subtract with up to 3 decimal places

Year: 5

2.7

?

5.43

2.7

?

$$\begin{array}{r} 4 \quad 1 \\ 5.43 \\ - 2.7 \\ \hline 2.73 \end{array}$$

5.43

5.43

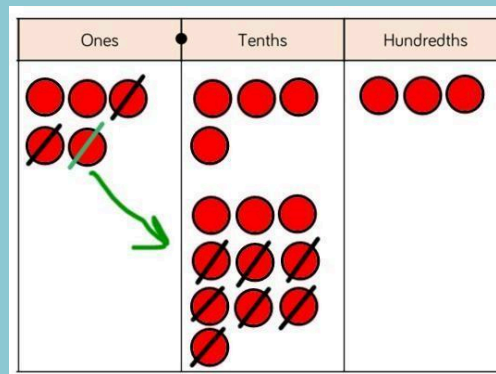
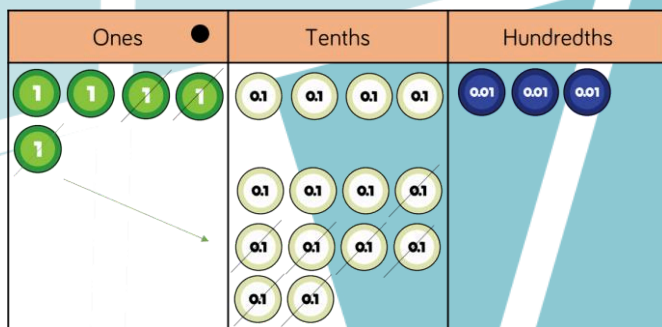
2.7

?

5.43    2.7    2.73

Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context when subtracting money and other measures.



Glossary

Year 1 - 6

Calculation Policy

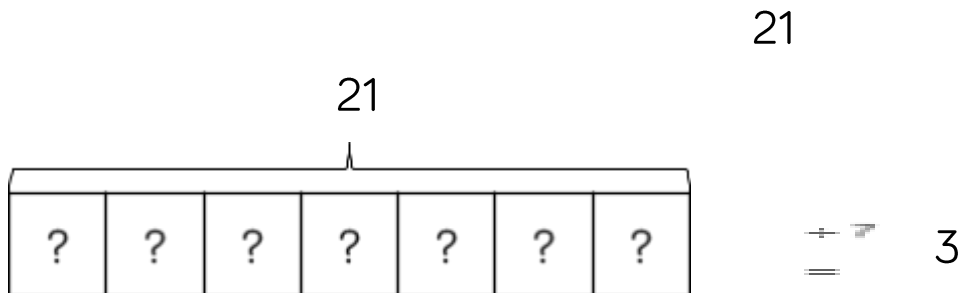
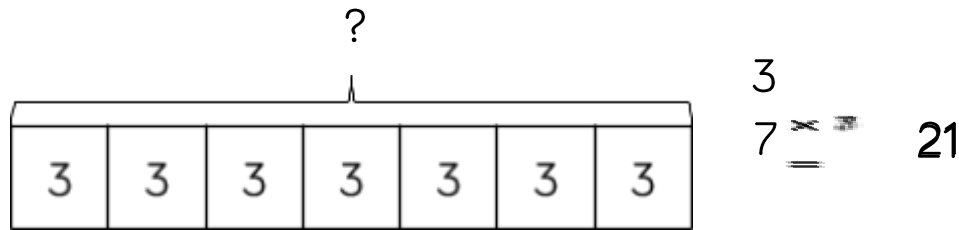
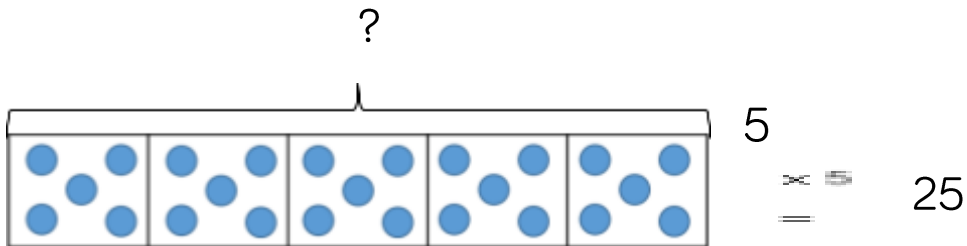
Multiplication and Division

[#MathsEveryoneCan](#)





# Bar Model



## Benefits

Children can use the single bar model to represent multiplication as repeated addition. They could use counters, cubes or dots within the bar model to support calculation before moving on to placing digits into the bar model to represent the multiplication.

Division can be represented by showing the total of the bar model and then dividing the bar model into equal groups.

It is important when solving word problems that the bar model represents the problem.

Sometimes, children may look at scaling problems. In this case, more than one bar model is useful to represent this type of problem, e.g. There are 3 girls in a group. There are 5 times more boys than girls. How many boys are there?

The multiple bar model provides an opportunity to compare the groups.



Boys

3	3	3	3	3
---	---	---	---	---

Girls

3
---

# Number Shapes



$$\begin{array}{r} 5 \\ 4 \\ \times \\ \hline 20 \\ 20 \\ \hline \end{array}$$



$$\begin{array}{r} 5 \\ 4 \\ \times \\ \hline 20 \\ 20 \\ \hline \end{array}$$



$$\begin{array}{r} + \\ \hline 6 \end{array}$$



## Benefits

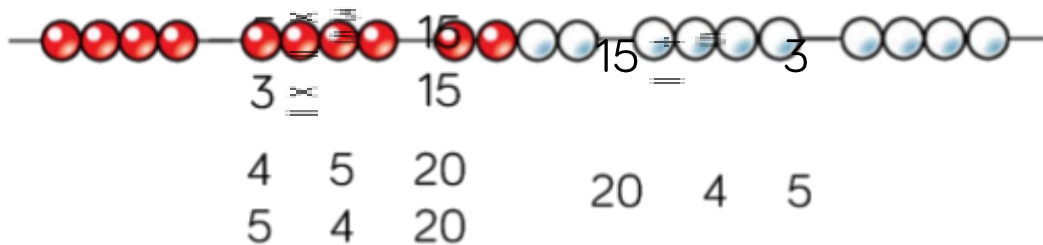
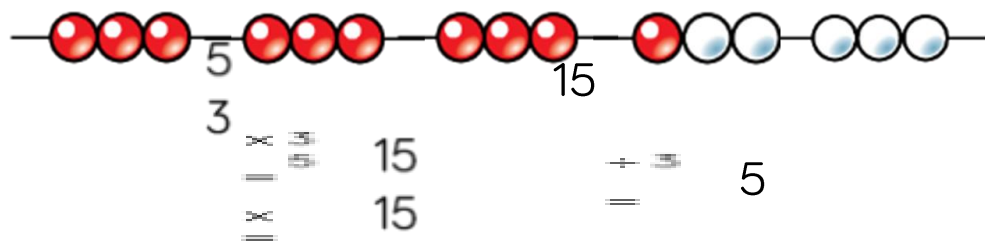
Number shapes support children's understanding of multiplication as repeated addition.

Children can build multiplications in a row using the number shapes. When using odd numbers, encourage children to interlock the shapes so there are no gaps in the row. They can then use the tens number shapes along with other necessary shapes over the top of the row to check the total. Using the number shapes in multiplication can support children in discovering patterns of multiplication e.g.  $\text{odd} \times \text{odd} = \text{even}$ ,  $\text{odd} \times \text{even} = \text{odd}$ ,  $\text{even} \times \text{even} = \text{even}$ .

When dividing, number shapes support children's understanding of division as grouping. Children make the number they are dividing and then place the number shape they are dividing by over the top of the number to find how many groups of the number there are altogether e.g. There are 6 groups of 3 in 18.



# Bead Strings



## Benefits

Bead strings to 100 can support children in their understanding of multiplication as repeated addition. Children can build the multiplication using the beads. The colour of beads supports children in seeing how many groups of 10 they have, to calculate the total more efficiently.

Encourage children to count in multiples as they build the number e.g. 4, 8, 12, 16, 20.

Children can also use the bead string to count forwards and backwards in multiples, moving the beads as they count.

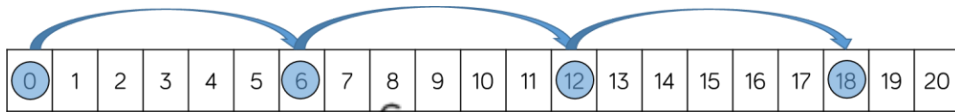
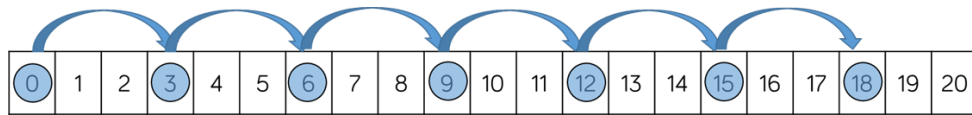
When dividing, children build the number they are dividing and then group the beads into the number they are dividing by e.g. 20 divided by 4 - Make 20 and then group the beads into groups of four. Count how many groups you have made to find the answer.

× =

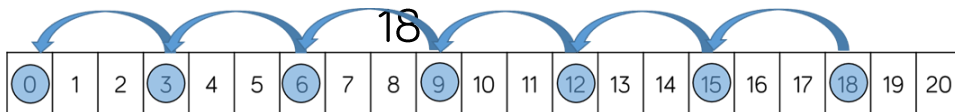
× =

÷ =

# Number Tracks



$$\begin{array}{r} 6 \\ \times 3 \\ \hline 18 \end{array}$$



$$\begin{array}{r} + 18 \\ \hline 6 \end{array}$$

## Benefits

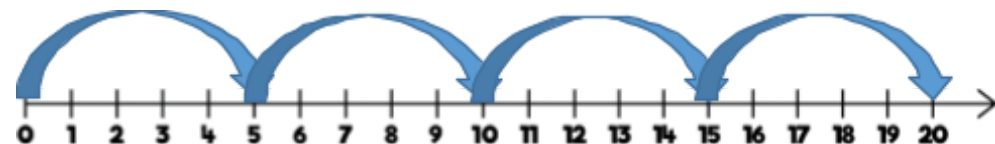
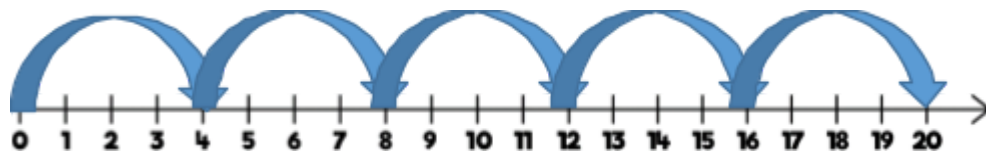
Number tracks are useful to support children to count in multiples, forwards and backwards. Moving counters or cubes along the number track can support children to keep track of their counting. Translucent counters help children to see the number they have landed on whilst counting.

When multiplying, children place their counter on 0 to start and then count on to find the product of the numbers.

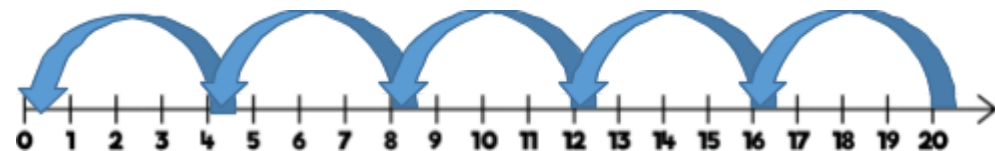
When dividing, children place their counter on the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0. Children record how many jumps they have made to find the answer to the division.

Number tracks can be useful with smaller multiples but when reaching larger numbers they can become less efficient.

# Number Lines (labelled)



$$\begin{array}{r} 5 \\ \times 4 \\ \hline 20 \end{array}$$



## Benefits

Labelled number lines are useful to support children to count in multiples, forwards and backwards as well as calculating single-digit multiplications.

When multiplying, children start at 0 and then count on to find the product of the numbers.

When dividing, start at the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0.

Children record how many jumps they have made to find the answer to the division.

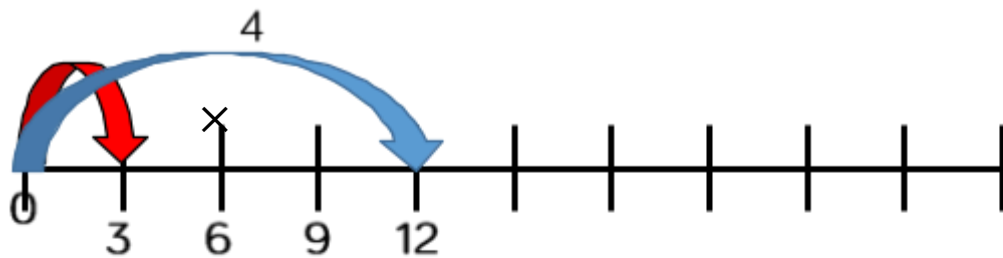
Labelled number lines can be useful with smaller multiples, however they become inefficient as numbers become larger due to the required size of the number line.



5



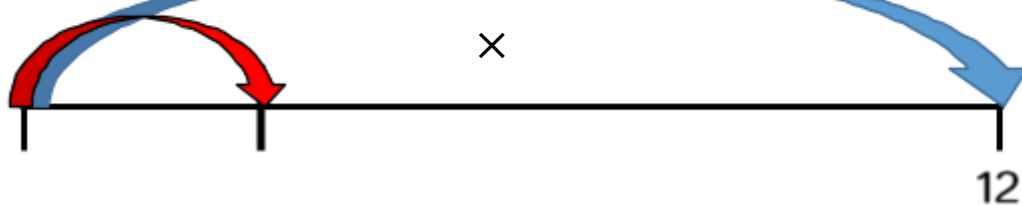
# Number Lines (blank)



A red car travels 3 miles.

A blue car 4 times further.

How far does the blue car travel?



## Benefits

Children can use blank number lines to represent scaling as multiplication or division.

Blank number lines with intervals can support children to represent scaling accurately. Children can label intervals with multiples to calculate scaling problems.

Blank number lines without intervals can also be used for children to represent scaling.

0







3

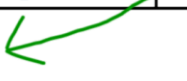
A blue car travels 12 miles.

A red car 4 times less.

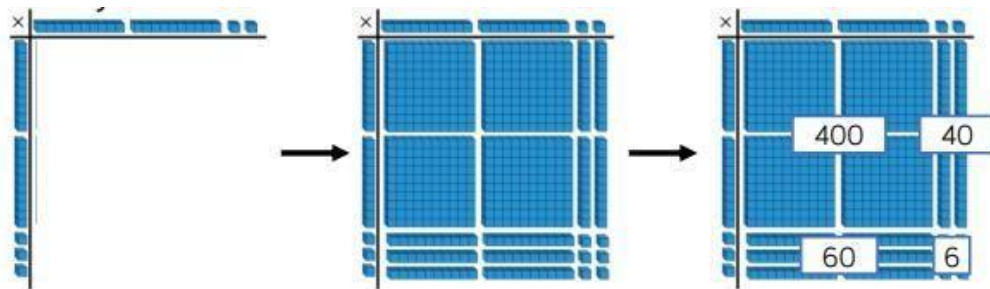
How far does the red car travel?

# Base 10/Dienes (multiplication)

Hundreds	Tens	Ones
		
		
		



$$\begin{array}{r}
 24 \\
 \times 3 \\
 \hline
 72 \\
 \hline
 1
 \end{array}$$



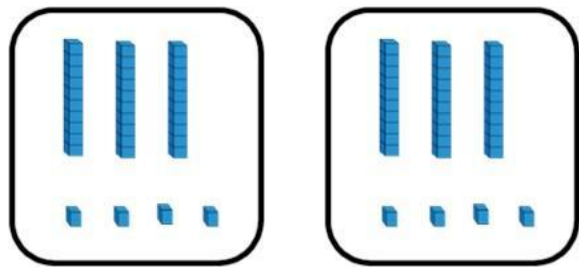
## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written representations match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed.

Base 10 also supports the area model of multiplication well. Children use the equipment to build the number in a rectangular shape which they then find the area of by calculating the total value of the pieces. This area model can be linked to the grid method or the formal column method of multiplying 2-digits by 2-digits.

# Base 10/Dienes (division)



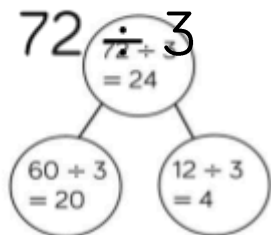
$$= 34$$

$$68 \div 2$$



Tens	Ones

$$= 24$$



## Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of division.

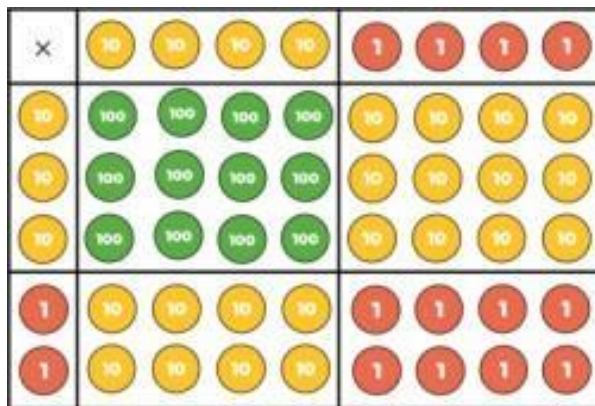
When numbers become larger, it can be an effective way to move children from representing numbers as ones towards representing them as tens and ones in order to divide. Children can then share the Base 10/ Dienes between different groups e.g. by drawing circles or by rows on a place value grid.

When they are sharing, children start with the larger place value and work from left to right. If there are any left in a column, they exchange e.g. one ten for ten ones. When recording, encourage children to use the part-whole model so they can consider how the number has been partitioned in order to divide. This will support them with mental methods.

# Place Value Counters (multiplication)



$$\begin{array}{r} 34 \\ \times 5 \\ \hline 170 \end{array}$$



$$\begin{array}{r} 44 \\ \times 32 \\ \hline 88 \\ 880 \\ + 1200 \\ \hline 1408 \end{array}$$

## Benefits

Using place value counters is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed. The counters should be used to support the understanding of the written method rather than support the arithmetic.

Place value counters also support the area model of multiplication well. Children can see how to multiply 2-digit numbers by 2-digit numbers.

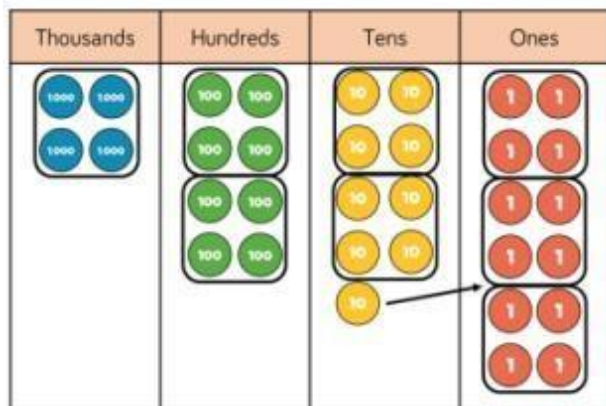
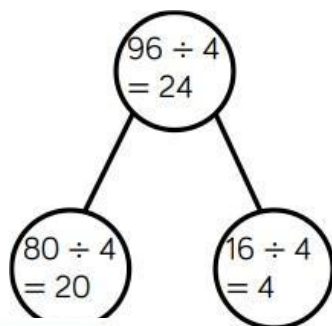
# Place Value Counters (division)

## Benefits

Using place value counters is an effective way to support children's understanding of division.

When working with smaller numbers, children can use place value counters to share between groups. They start by sharing the larger place value column and work from left to right. If there are any counters left over once they have been shared, they exchange the counter e.g. exchange one ten for ten ones. This method can be linked to the part-whole model to support children to show their thinking.

Place value counters also support children's understanding of short division by grouping the counters rather than sharing them. Children work from left to right through the place value columns and group the counters in the number they are dividing by. If there are any counters left over after they have been grouped, they exchange the counter e.g. exchange one hundred for ten tens.



$$4 \overline{) 4892}$$

# Times Tables



Skill	Year	Representations and models	
Recall and use multiplication and division facts for the 2-times table	2	Bar model Number shapes Counters Money	Ten frames Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 5-times table	2	Bar model Number shapes Counters Money	Ten frames Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 10-times table	2	Hundred square Number shapes Counters Money	Ten frames Bead strings Number lines Base 10

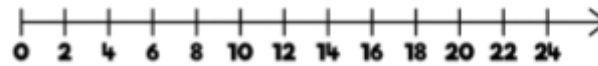
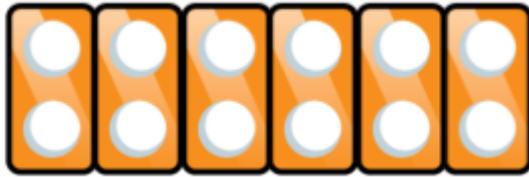


Skill	Year	Representations and models	
Recall and use multiplication and division facts for the 3-times table	3	Hundred square Number shapes Counters	Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 4-times table	3	Hundred square Number shapes Counters	Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 8-times table	3	Hundred square Number shapes	Bead strings Number tracks Everyday objects
Recall and use multiplication and division facts for the 6-times table	4	Hundred square Number shapes	Bead strings Number tracks Everyday objects

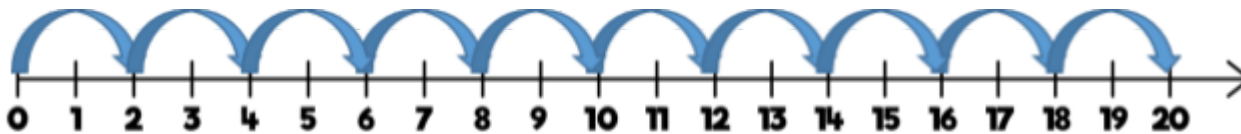
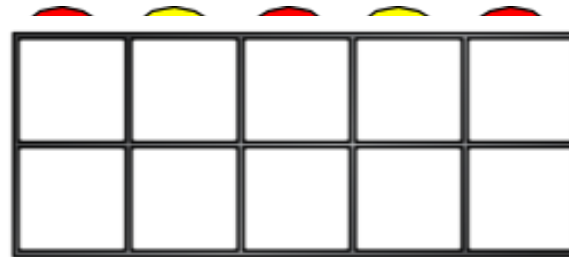
Skill	Year	Representations and models	
Recall and use multiplication and division facts for the 7-times table	4	Hundred square Number shapes	Bead strings Number lines
Recall and use multiplication and division facts for the 9-times table	4	Hundred square Number shapes	Bead strings Number lines
Recall and use multiplication and division facts for the 11-times table	4	Hundred square Base 10	Place value counters Number lines
Recall and use multiplication and division facts for the 12-times table	4	Hundred square Base 10	Place value counters Number lines

## Skill: 2 times table

Year: 2



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50



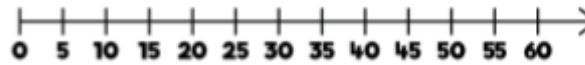
Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the two times table, using concrete manipulatives to support. Notice how all the numbers are even and there is a pattern in the ones.

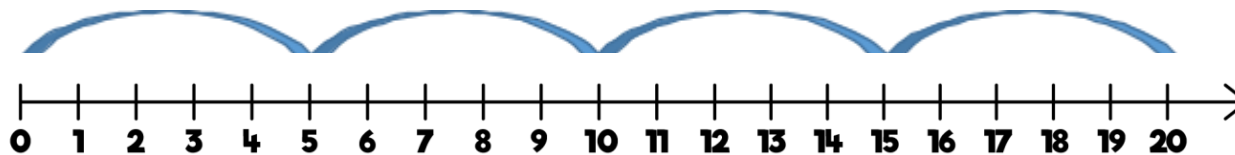
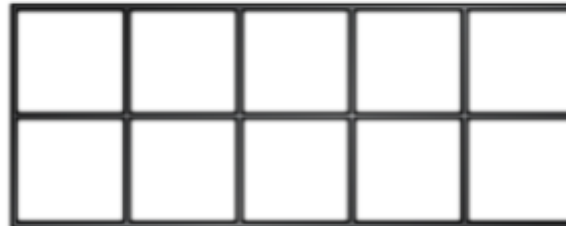
Use different models to develop fluency.

## Skill: 5 times table

Year: 2



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

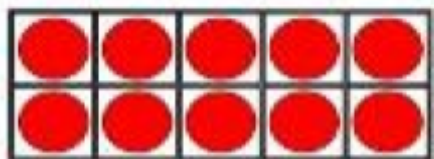
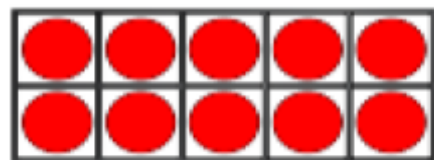
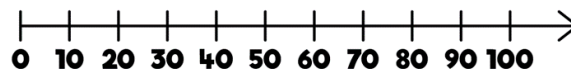


Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the five times table, using concrete manipulatives to support. Notice the pattern in the ones as well as highlighting the odd, even, odd, even pattern.

## Skill: 10 times table

Year: 2



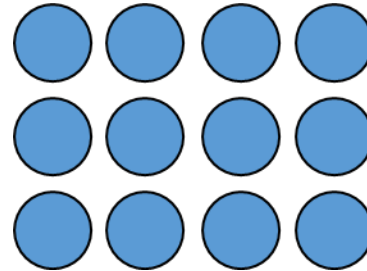
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

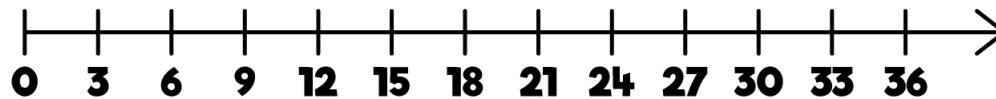
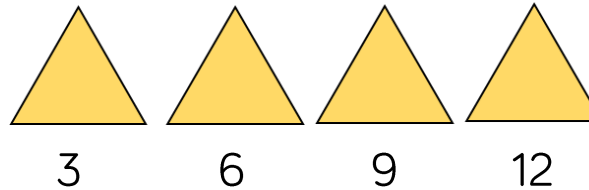
Look for patterns in the ten times table, using concrete manipulatives to support. Notice the pattern in the digits- the ones are always 0, and the tens increase by 1 ten each time.

## Skill: 3 times table

Year: 3



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50



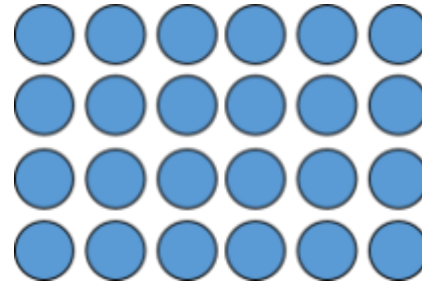
Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the three times table, using concrete manipulatives to support. Notice the odd, even, odd, even pattern using number shapes to support. Highlight the pattern in the ones using a hundred square.

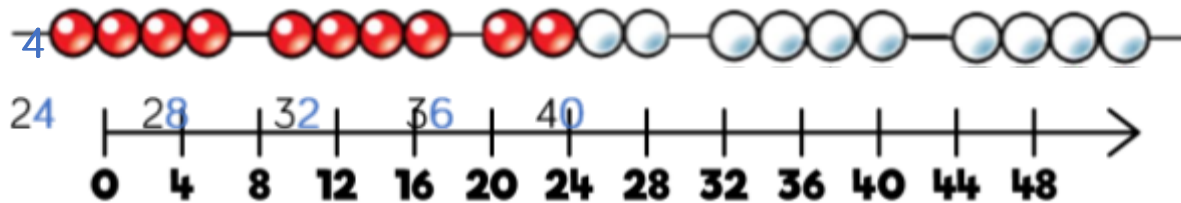
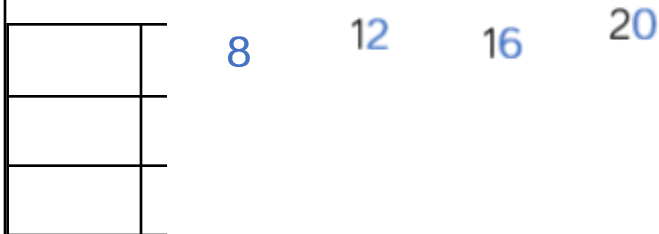
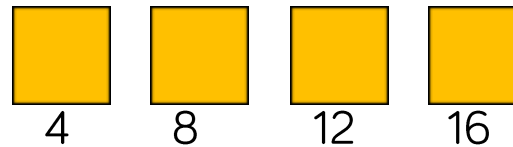


## Skill: 4 times table

Year: 3

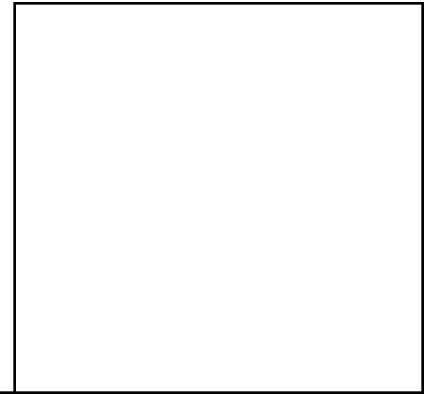


1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50



Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the four times table, using manipulatives to support. Make links to the 2 times table, seeing how each multiple is double the twos. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

44 48 52 56 60

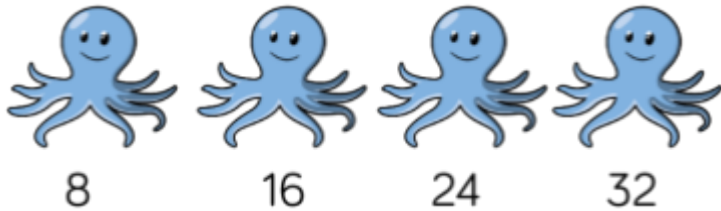




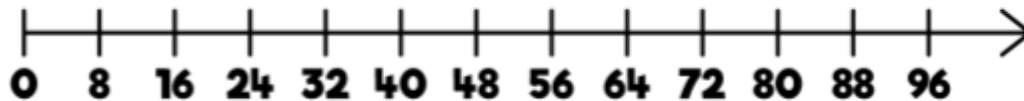
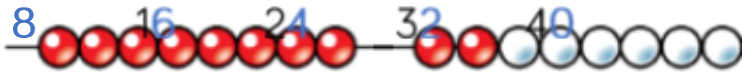

1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

### Skill: 8 times table

Year: 3



31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



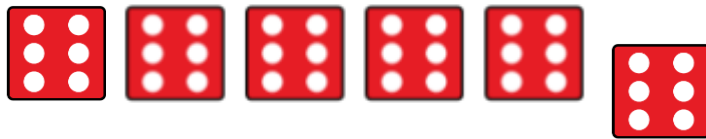
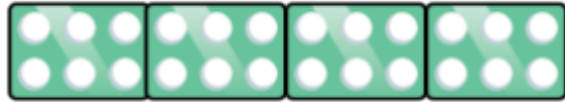
48 56 64 72 80



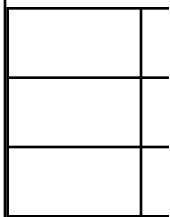
Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the eight times table, using manipulatives to support. Make links to the 4 times table, seeing how each multiple is double the fours. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

## Skill: 6 times table

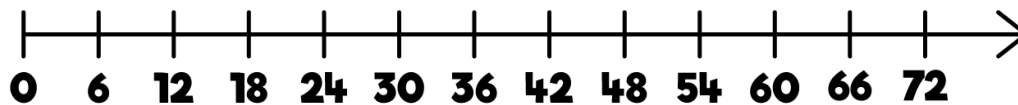
Year: 4



12      18      24      30



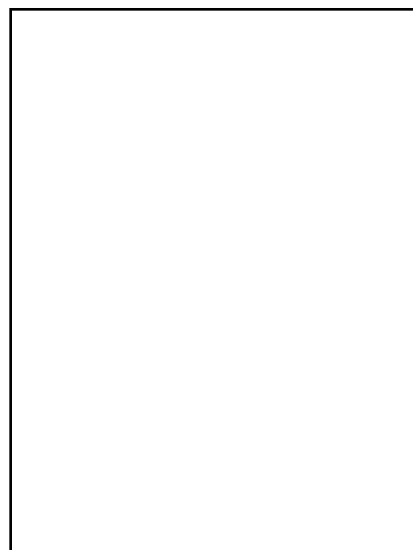
6



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the six times table, using manipulatives to support. Make links to the 3 times table, seeing how each multiple is double the threes. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

66 72 78 84 90



## Skill: 9 times table

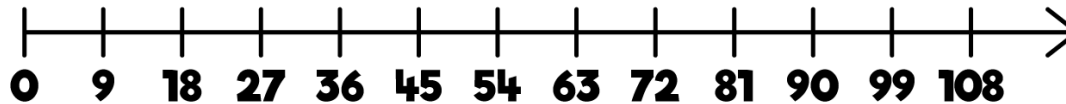
Year: 4




18      27      36      45

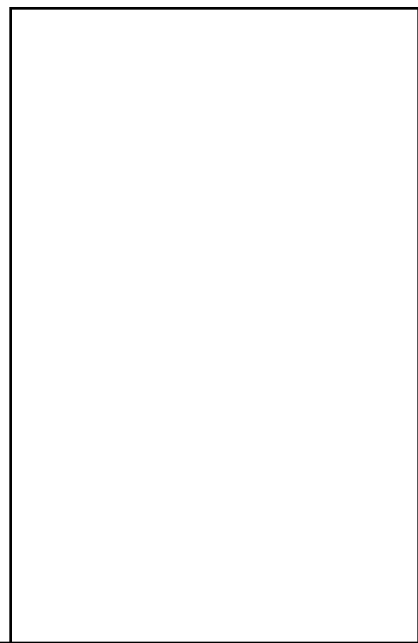
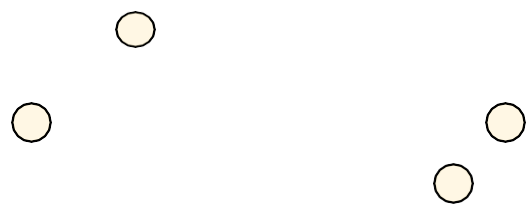
9

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd, even pattern within the multiples.

54 63 72 81 90





42

49

56

63

70



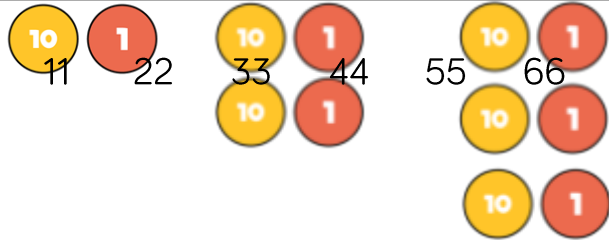
Encourage daily counting in multiples both forwards and backwards, supported by a number line or a hundred square. The seven times table can be trickier to learn due to the lack of obvious pattern in the numbers, however they already know several facts due to commutativity. Children can still see the odd, even pattern in the multiples using number shapes to support.




1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	----

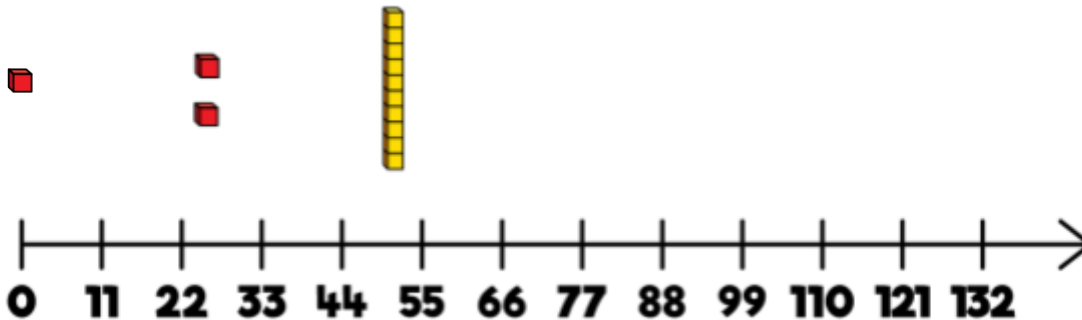
### Skill: 11 times table

Year: 4

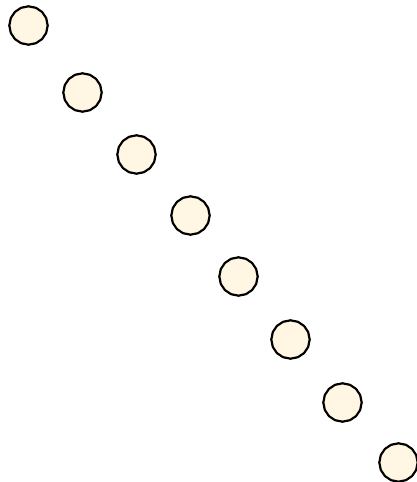


41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.



77    88    99    110    121    132



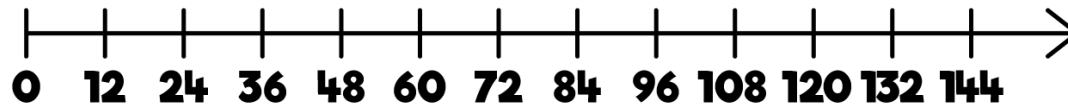
Look for patterns in the eleven times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support. Also consider the pattern after crossing 100


1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30

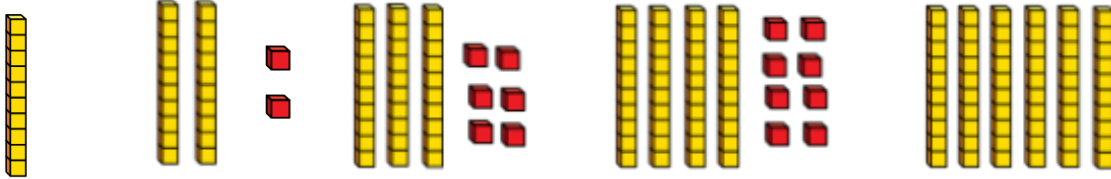
### Skill: 12 times table

Year: 4

51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



132 144



Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the 12 times table, using manipulatives to support. Make links to the 6 times table, seeing how each multiple is double the sixes. Notice the pattern in the ones within each group of five multiples. The hundred square can support in highlighting this pattern.

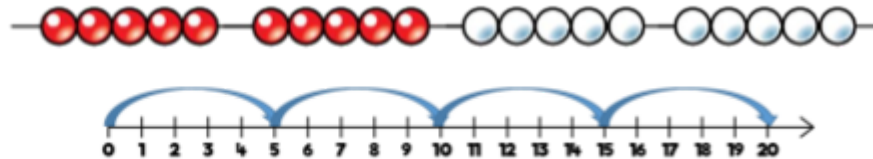
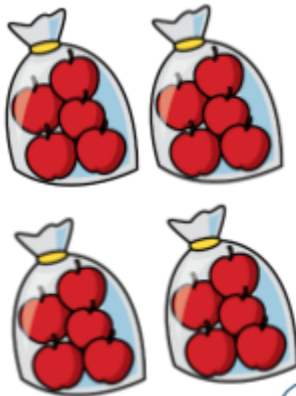
# Multiplication

Skill	Year	Representations and models	
Solve one-step problems with multiplication	1/2	Bar model Number shapes Counters	Ten frames Bead strings Number lines
Multiply 2-digit by 1-digit numbers	3/4	Place value counters Base 10	Short written method Expanded written method
Multiply 3-digit by 1-digit numbers	4	Place value counters Base 10	Short written method
Multiply 4-digit by 1-digit numbers	5	Place value counters	Short written method

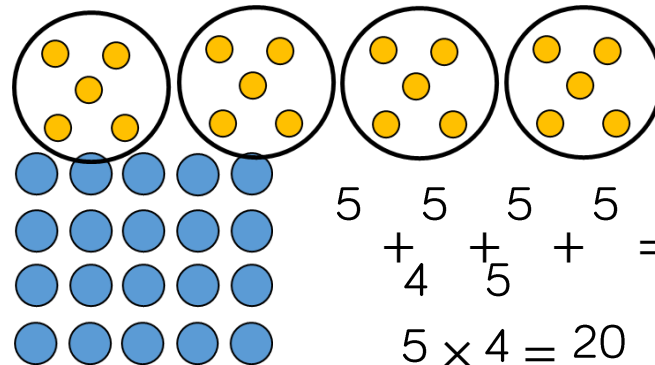
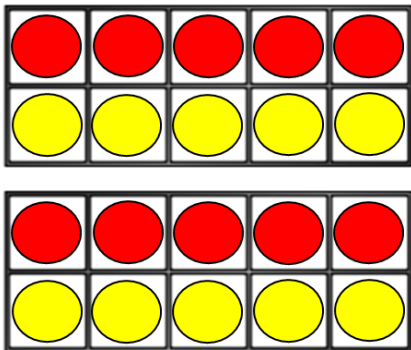
Skill	Year	Representations and models	
Multiply 2-digit by 2-digit numbers	5	Place value counters Base 10	Short written method Grid method
Multiply 2-digit by 3-digit numbers	5	Place value counters	Short written method Grid method
Multiply 2-digit by 4-digit numbers	5/6	Formal written method	

Skill: Solve 1-step problems using multiplication

Year: 1/2



One bag holds 5 apples.  
How many apples do 4 bags hold?



$$\begin{array}{r} 5 \\ + 5 \\ + 5 \\ + 5 \\ \hline 20 \end{array}$$

$$5 \times 4 = 20$$

$$\begin{array}{r} \phantom{5} \\ \times 4 \\ \hline 20 \end{array}$$

Children represent multiplication as repeated addition in many different ways.

In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record multiplication formally.

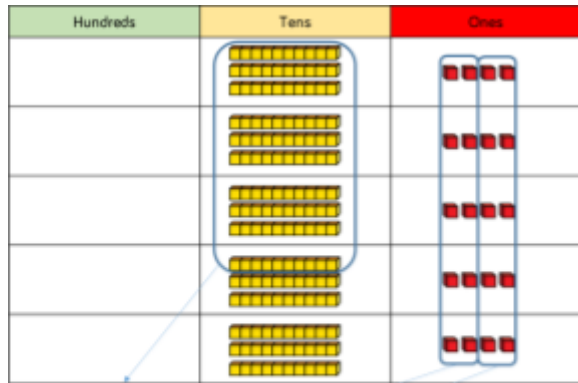
In Year 2, children are introduced to the multiplication symbol.



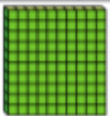


## Skill: Multiply 2-digit numbers by 1-digit numbers

Year: 3/4

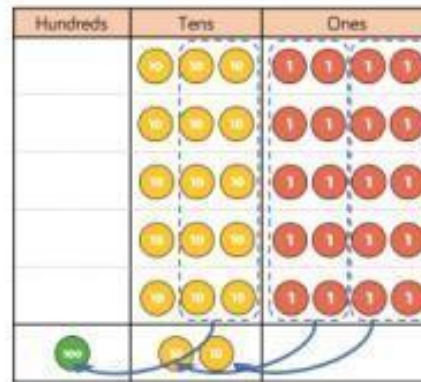


	H	T	O	
		3	4	
x			5	
		2	0	(5 × 4)
+	1	5	0	(5 × 30)
	1	7	0	



$$34 \times 5 = 170$$

	H	T	O
		3	4
x			5
	1	7	0
	1	2	

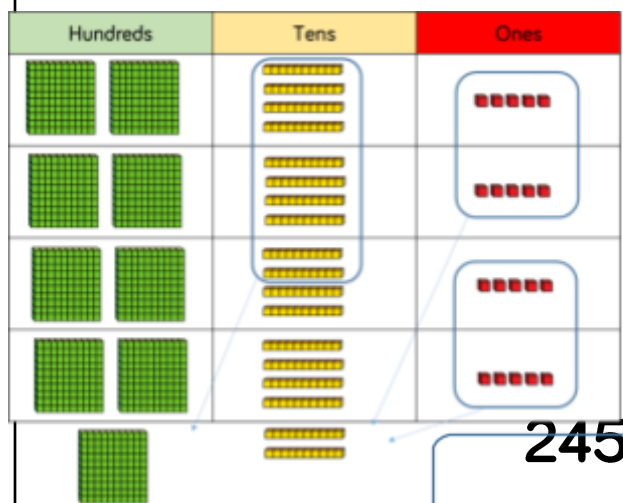


Teachers may decide to first look at the expanded column method before moving on to the short multiplication method.

The place value counters should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge.

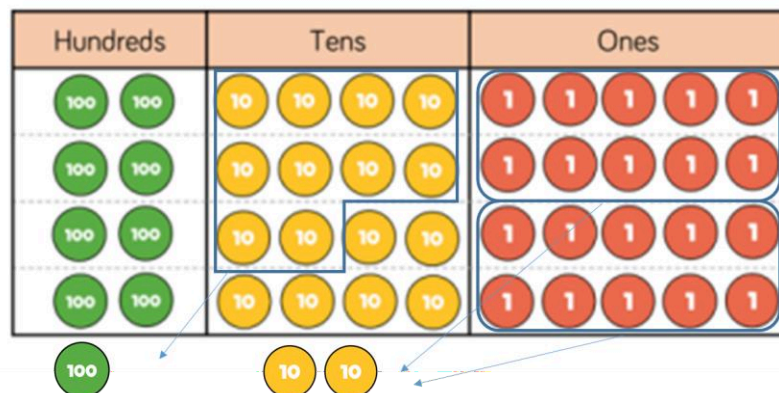
## Skill: Multiply 3-digit numbers by 1-digit numbers

Year: 3/4



	H	T	O
	2	4	5
x			4
	9	8	0
	1	2	

$$\begin{array}{r} 245 \\ \times 4 \\ \hline 980 \end{array}$$

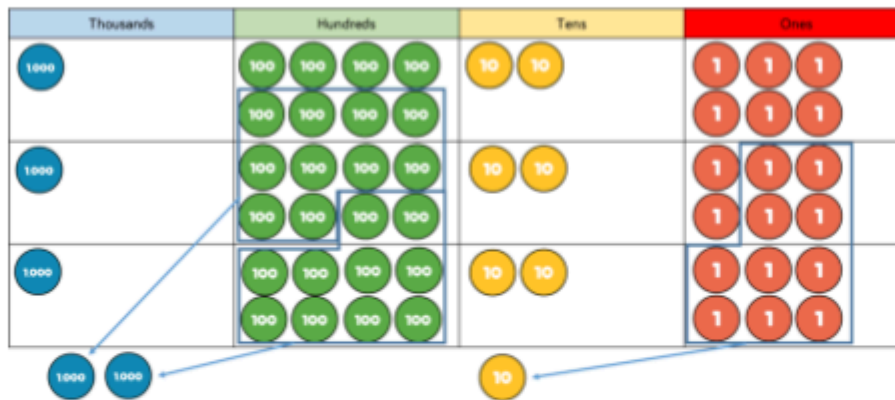


When moving to 3-digit by 1-digit multiplication, encourage children to move towards the short, formal written method.

Base 10 and place value counters continue to support the understanding of the written method. Limit the number of exchanges needed in the questions and move children away from resources when multiplying larger numbers.

## Skill: Multiply 4-digit numbers by 1-digit numbers

Year: 5



$$1,826 \quad 3 \quad 5,478$$

$$2 \times 3 = 6$$

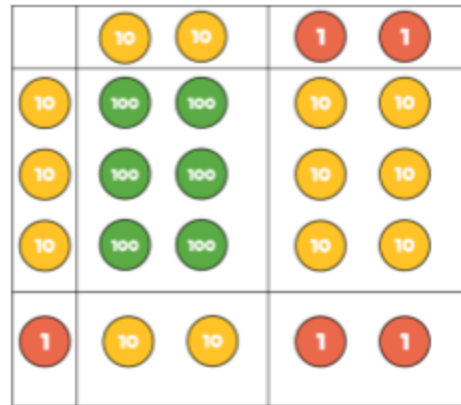
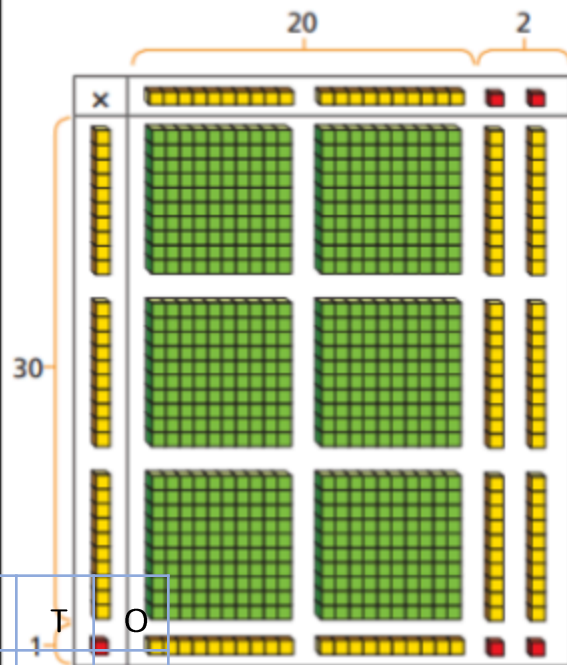
Th H T O

When multiplying 4-digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method. If children are multiplying larger numbers and struggling with their times tables, encourage the use of multiplication grids so children can focus on the use of the written method.

	1	8	2	6
×				3
	5	4	7	8

## Skill: Multiply 2-digit numbers by 2-digit numbers

Year: 5



	20	2
30	600	60
1	20	2

	H	T	O
		1	
		2	2
×		3	1
		2	2
	6	6	0
	6	8	2

**22 31 682**

When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding the space covered by the Base 10.

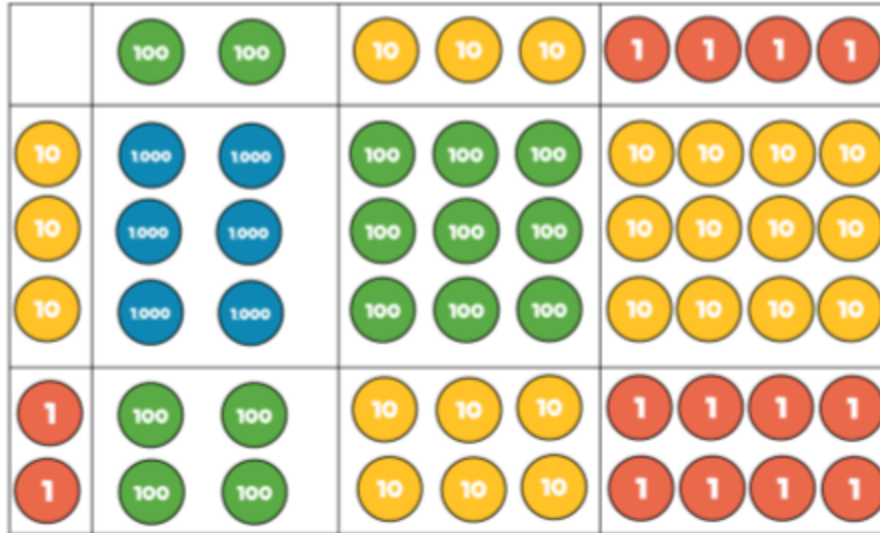
The grid method matches the area model as an initial written method before moving on to the formal written multiplication method.

×

× =

## Skill: Multiply 3-digit numbers by 2-digit numbers

Year: 5



234    32    7,488

		Th	H	T	O
×	200	30	2	3	4
30	6,000	×	900	3	120
2	400		60	6	8

	Th	H	T	O
	1	7	1	0
	7			

Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.

Encourage children to move towards the formal written method, seeing the links with the grid method.



× =

## Skill: Multiply 4-digit numbers by 2-digit numbers

Year: 5/6

	TTh	Th	H	T	O
		2	7	3	9
×				2	8
<hr/>					
2	1	9	1	2	
2	5	3	7		
<hr/>					
5	4	1	7	8	0
1					
<hr/>					
7	6	6	9	2	

2,739    28    76,692

When multiplying 4-digits by 2-digits, children should be confident in the written method.

If they are still struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method.

Consider where exchanged digits are placed and make sure this is consistent.

× =

**Division**

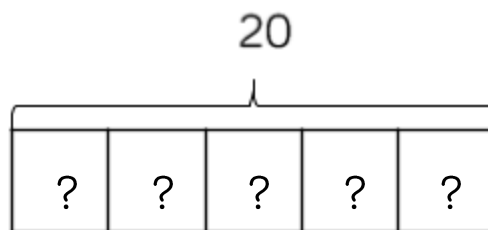
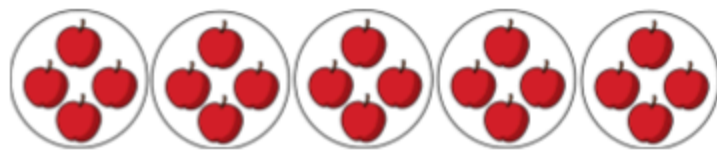
Skill	Year	Representations and models
Solve one-step problems with division (sharing)	1/2	Bar model Real life objects Arrays Counters
Solve one-step problems with division (grouping)	1/2	Real life objects Number shapes Bead strings Ten frames Number lines Arrays Counters
Divide 2-digits by 1-digit (no exchange sharing)	3	Straws Base 10 Bar model Place value counters Part-whole model
Divide 2-digits by 1-digit (sharing with exchange)	3	Straws Base 10 Bar model Place value counters Part-whole model

Skill	Year	Representations and models	
Divide 2-digits by 1-digit (sharing with remainders)	3/4	Straws Base 10 Bar model	Place value counters Part-whole model
Divide 2-digits by 1-digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division
Divide 3-digits by 1-digit (sharing with exchange)	4	Base 10 Bar model	Place value counters Part-whole model
Divide 3-digits by 1-digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division

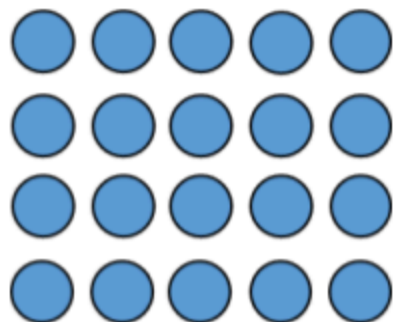
Skill	Year	Representations and models	
Divide 4-digits by 1-digit (grouping)	5	Place value counters Counters	Place value grid Written short division
Divide multi-digits by 2-digits (short division)	6	Written short division	List of multiples
Divide multi-digits by 2-digits (long division)	6	Written long division	List of multiples

Skill: Solve 1-step problems using multiplication (sharing)

Year: 1/2



There are 20 apples altogether.  
They are shared equally between 5 bags.  
How many apples are in each bag?



$$20 \div 5 = \square$$

Children solve problems by sharing amounts into equal groups.

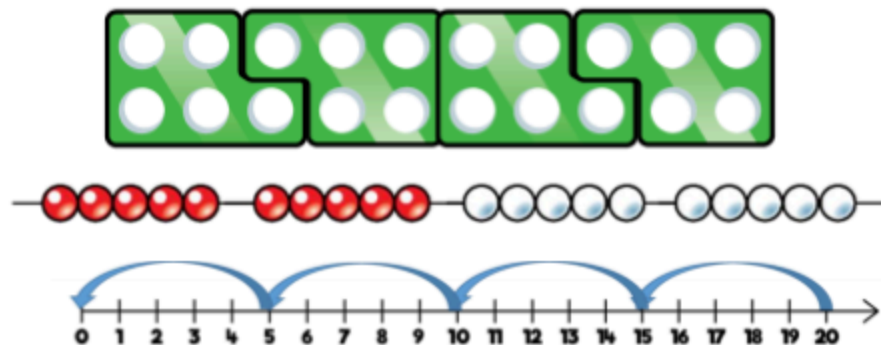
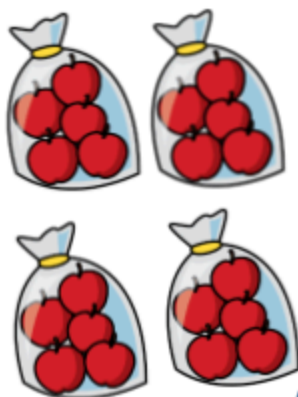
In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record division formally.

In Year 2, children are introduced to the division symbol.

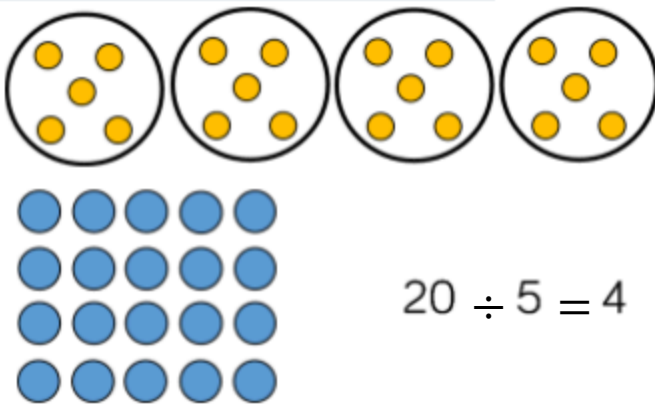
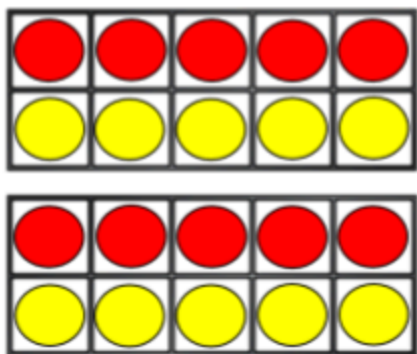


**Skill: Solve 1-step problems using division (grouping)**

**Year: 1/2**



There are 20 apples altogether.  
They are put in bags of 5.  
How many bags are there?



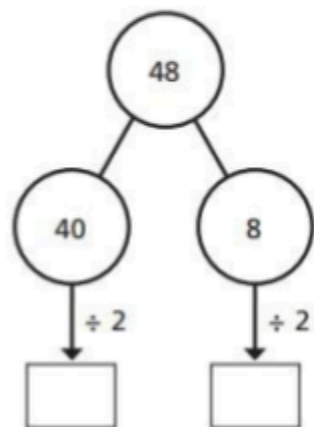
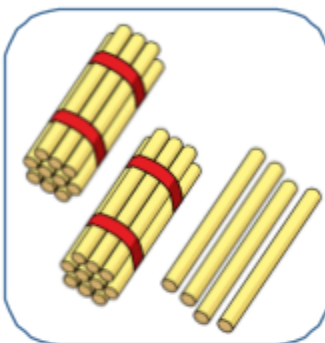
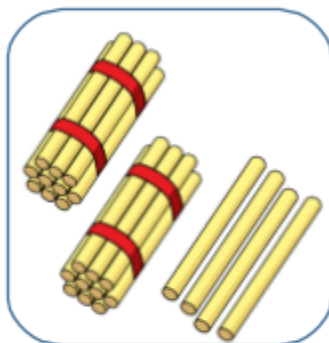
$$20 \div 5 = 4$$

Children solve problems by grouping and counting the number of groups. Grouping encourages children to count in multiples and links to repeated subtraction on a number line. They can use concrete representations in fixed groups such as number shapes which helps to show the link between multiplication and division.

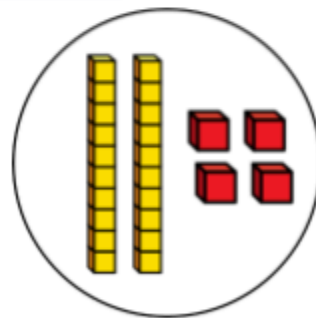
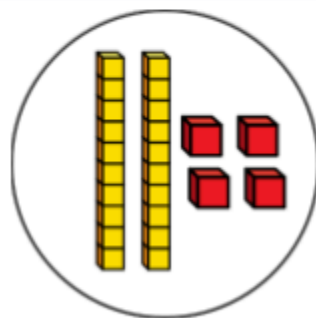
## Skill: Divide 2-digits by 1-digit (sharing with no exchange)

Year: 1/2

Tens	Ones
10 10	1 1 1 1
10 10	1 1 1 1



$$48 \div 2 = 24$$



When dividing larger numbers, children can use manipulatives that allow them to partition into tens and ones.









Straws, Base 10 and place value counters can all be used to share numbers into equal groups.

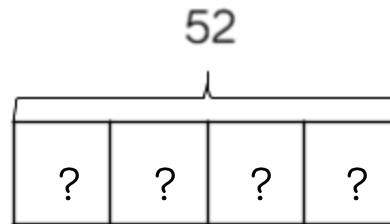
Part-whole models can provide children with a clear written method that matches the concrete representation.

## Skill: Divide 2-digits by 1-digit (sharing with exchange)

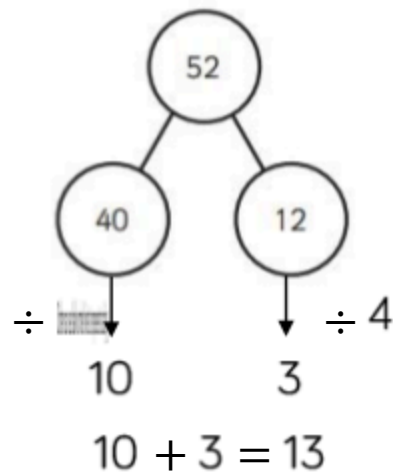
Year: 3/4











Tens	Ones
	
	
	
	



$$52 \div 4 = 13$$



Tens	Ones
	
	
	
	

When dividing numbers involving an exchange, children can use Base 10 and place value counters to exchange one ten for ten ones.









Children should start with the equipment outside the place value grid before sharing the tens and ones equally between the rows.

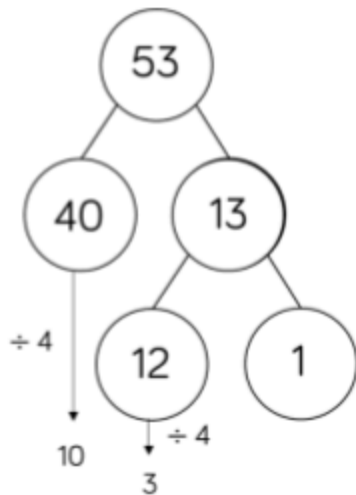
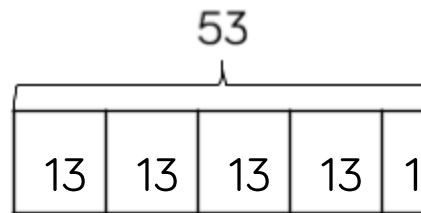
Flexible partitioning in a part-whole model supports this method.

## Skill: Divide 2-digits by 1-digit (sharing with remainders)








Year: 3/4



Tens	Ones
	
	
	
	



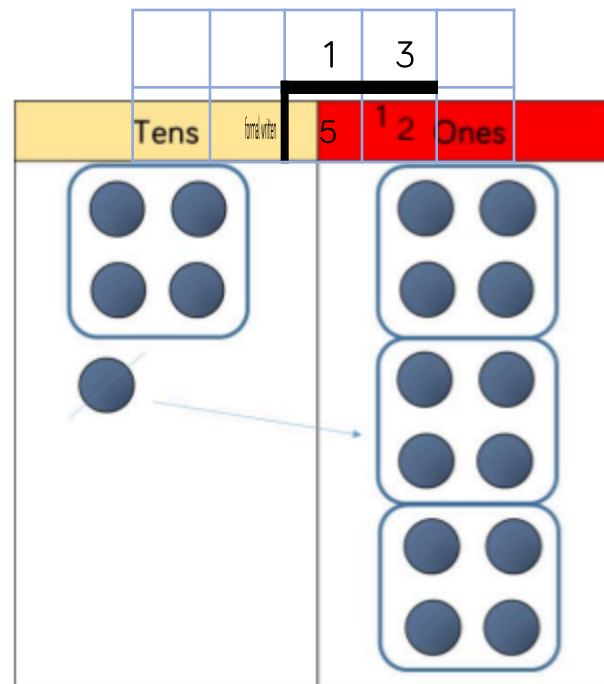
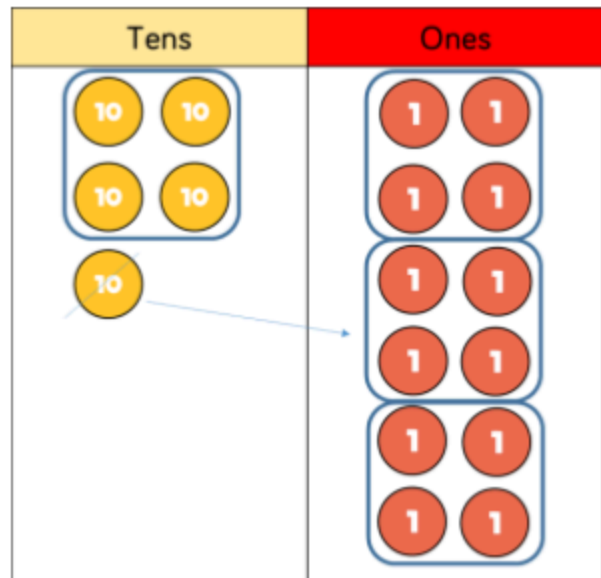
$$53 \div 4 = 13 \text{ r}1$$

Tens	Ones
	
	
	
	

When dividing numbers with remainders, children can use Base 10 and place value counters to exchange one ten for ten ones. Starting with the equipment outside the place value grid will highlight remainders, as they will be left outside the grid once the equal groups have been made. Flexible partitioning in a part-whole model supports this method.

## Skill: Divide 2-digits by 1-digit (grouping)

Year: 4/5



$$52 \div 4 = 13$$

÷ =

When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor.

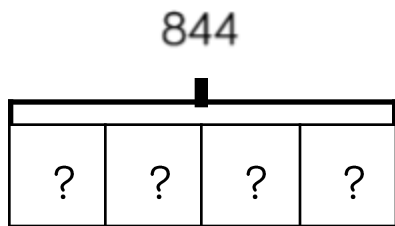
Language is important here. Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'

Remainders can also be seen as they are left ungrouped.

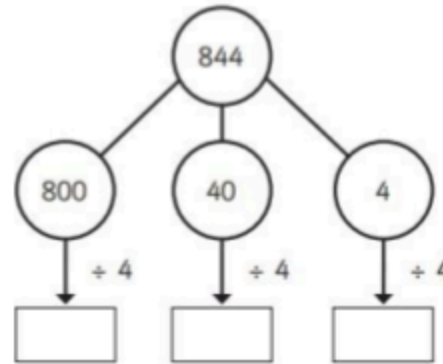
## Skill: Divide 3-digits by 1-digit (sharing)

Year: 4

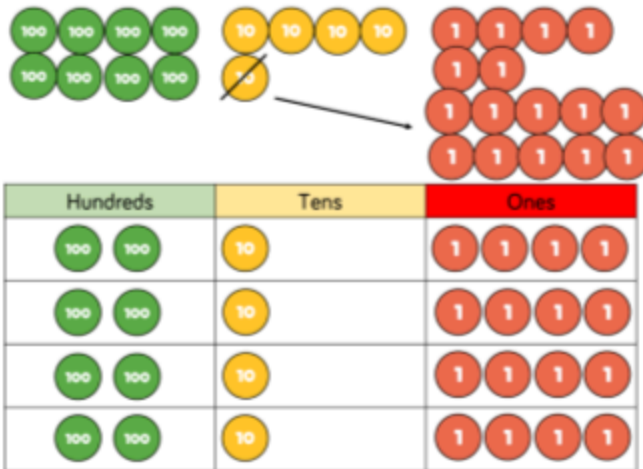
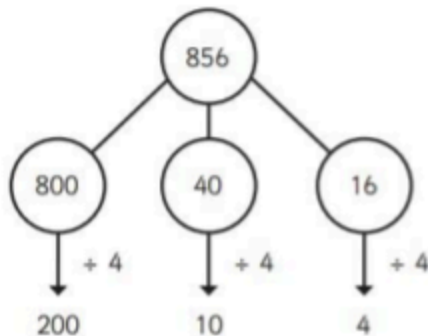
$$844 \div 4 = 211$$



H	T	O



$$844 \div 4 = 211$$

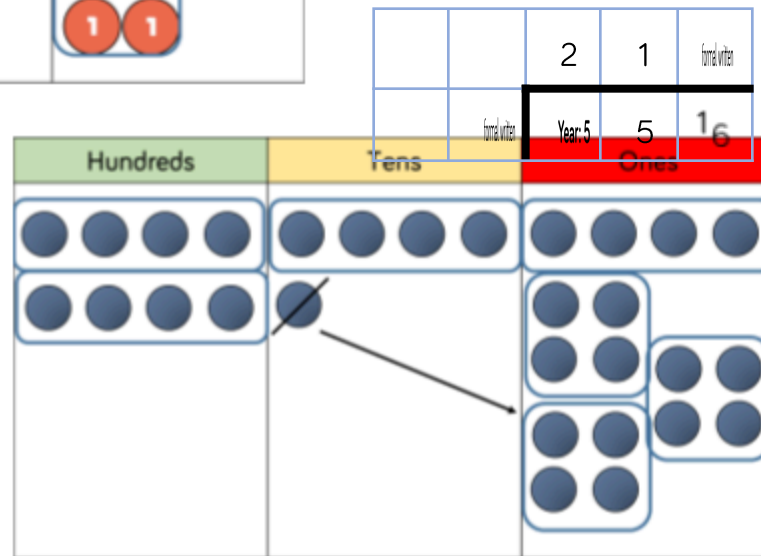


Children can continue to use place value counters to share 3-digit numbers into equal groups. Children should start with the equipment outside the place value grid before sharing the hundreds, tens and ones equally between the rows. This method can also help to highlight remainders. Flexible partitioning in a part-whole model supports this method.



## Skill: Divide 3-digits by 1-digit (grouping)

Year: 5



856    4    214

Children can continue to use grouping to support their understanding of short division when dividing a 3-digit number by a 1-digit number.

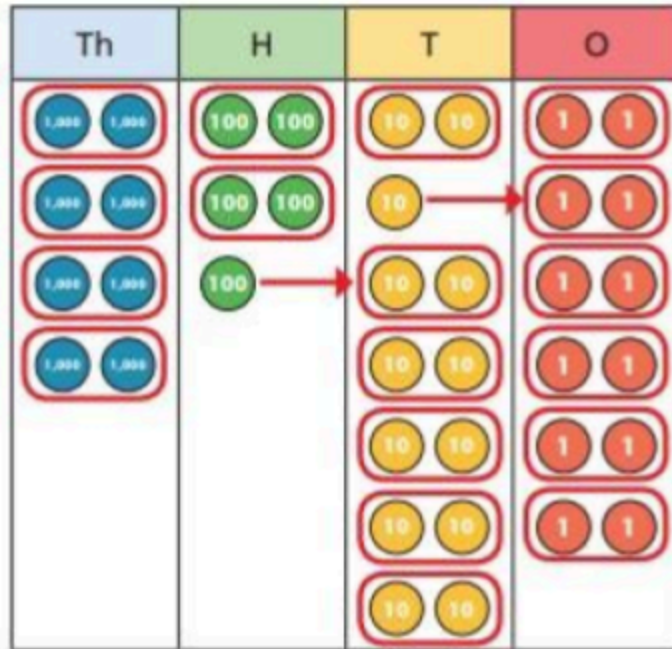
Place value counters or plain counters can be used on a place value grid to support this understanding. Children can also draw their own counters and group them through a more pictorial method.

÷ =



## Skill: Divide 4-digits by 1-digit (grouping)

Year: 5



	formal	2	6	6
2	Year: 5	5	13	12

$$8,532 \div 2 = 4,266$$

Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1-digit. Children can also draw their own counters and group them through a more pictorial method.

Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.

$$\div =$$

## Skill: Divide multi digits by 2-digits (short division)

Year: 6

432 12 36

	0	3	6	
12				

4 3 7 2

7,335 15 489

÷ =

When children begin to divide up to 4-digits by 2-digits, written methods become the most accurate as concrete and pictorial representations become less effective. Children can write out multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient can be rounded as appropriate.

	0	found water	Year: 5	9								
15	7											

$7_3$     $13_3$     $13_5$

$\div$     $=$

- 15   30   45   60   75   90   105   120   135   150

## Skill: Divide multi-digits by 2-digits (long division)

Year: 6

		0	3	6
1	2	4	3	2
	-	3	6	0
			7	2
	-		7	2
				0

$12 \times 1 = 12$   
 $12 \times 2 = 24$   
 $12 \times 3 = 36$   
 $12 \times 4 = 48$   
 $12 \times 5 = 60$   
 $12 \times 6 = 72$   
 $12 \times 7 = 84$   
 $12 \times 8 = 96$   
 $12 \times 7 = 108$   
 $12 \times 10 = 120$

$$432 \quad 12 \overline{) 36}$$

$$7,335 \quad 15 \overline{) 489}$$

		0	4	8	9
15		7	3	3	5
-		6	0	0	0
		1	3	3	5
-		1	2	0	0
			1	3	5
-			1	3	5
					0

$1 \times 15 = 15$   
 $2 \times 15 = 30$   
 $3 \times 15 = 45$   
 $4 \times 15 = 60$   
 $5 \times 15 = 75$   
 $10 \times 15 = 150$

Children can also divide by 2-digit numbers using long division.

Children can write out multiples to support their calculations with larger remainders.

Children will also solve problems with remainders where the quotient can be rounded as appropriate.

### Skill: Divide multi digits by 2-digits (long division)

Year: 6

$$372 \quad 15 \quad 24 \text{ r}12$$

$$\div =$$

			2	4	r	1	2
1	5	3	7	2			
	-	3	0	0			
			7	2			
	-		6	0			
			1	2			

$1 \times 15 = 15$

$2 \times 15 = 30$

$3 \times 15 = 45$

$4 \times 15 = 60$

$5 \times 15 = 75$

$10 \times 15 = 150$

When a remainder is left at the end of a calculation, children can either leave it as a remainder or convert it to a fraction. This will depend on the context of the question.

			2	4	$\frac{4}{5}$
1	5	3	7	2	
	-	3	0	0	
			7	2	
	-		6	0	
			1	2	

$$372 \quad 15 \quad 24 \frac{4}{5}$$

$$\div =$$

Children can also answer questions where the quotient needs to be rounded according to the context.

# Glossary

**Addend** - A number to be added to another.

**Aggregation** - combining two or more quantities or measures to find a total.

**Augmentation** - increasing a quantity or measure by another quantity.

**Commutative** - numbers can be added in any order.

**Complement** - in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000

**Difference** - the numerical difference between two numbers is found by comparing the quantity in each group.

**Exchange** - Change a number or expression for another of an equal value.

**Minuend** - A quantity or number from which another is subtracted.

**Partitioning** - Splitting a number into its component parts.

**Reduction** - Subtraction as take away.

**Subitise** - Instantly recognise the number of objects in a small group without needing to count.

**Subtrahend** - A number to be subtracted from another.

**Sum** - The result of an addition.

**Total** - The aggregate or the sum found by addition.

**Array** – An ordered collection of counters, cubes or other item in rows and columns.

**Commutative** – Numbers can be multiplied in any order.

**Dividend** – In division, the number that is divided.

**Divisor** – In division, the number by which another is divided.

**Exchange** – Change a number or expression for another of an equal value.

**Factor** – A number that multiplies with another to make a product.

**Multiplicand** – In multiplication, a number to be multiplied by another.

**Partitioning** – Splitting a number into its component parts.

**Product** – The result of multiplying one number by another.

**Quotient** – The result of a division

**Remainder** – The amount left over after a division when the divisor is not a factor of the dividend.

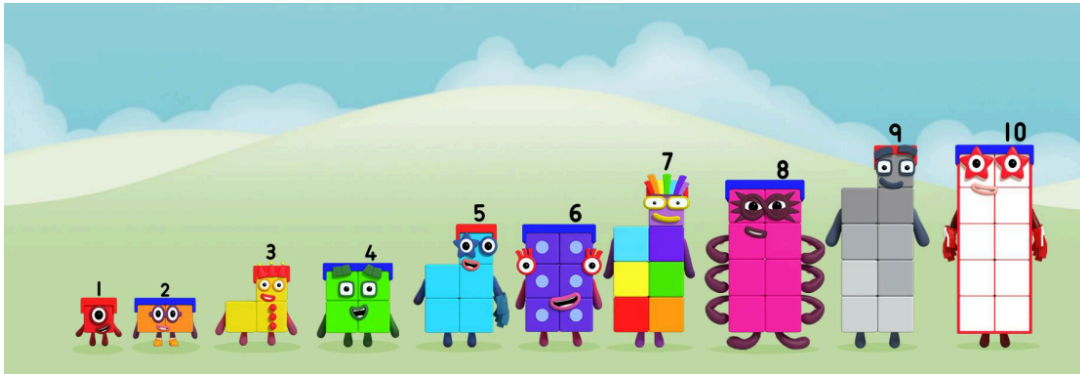
**Scaling** – Enlarging or reducing a number by a given amount, called the scale factor



## Appendix

### Representations to support Maths in EYFS

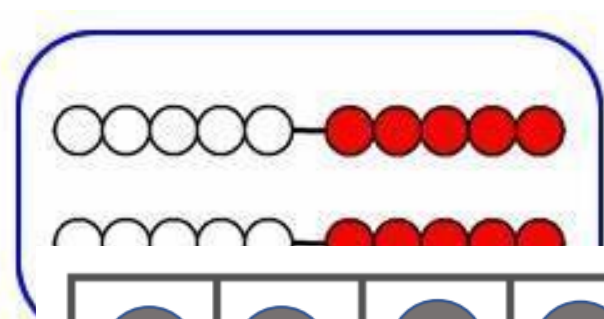
Number Blocks



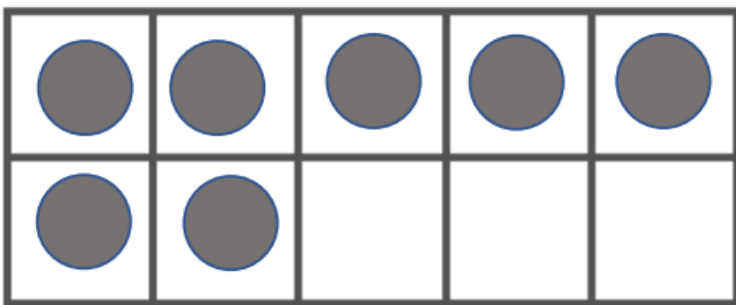
Numicon



Rekenrek



Number Track



## Tens Frame